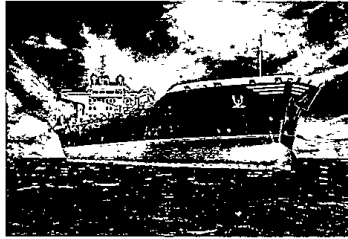


# Candidate 1 evidence

SECTION 1 — 20 marks

Attempt ALL questions

1. A new material is being tested for use in the manufacture of ships.



The results of a tensile test on the material are shown in Figure 1.

The range of 0 to A is shown magnified in Figure 2.

Figure 1

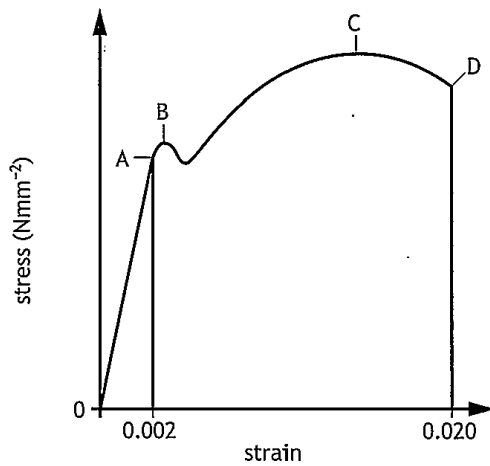
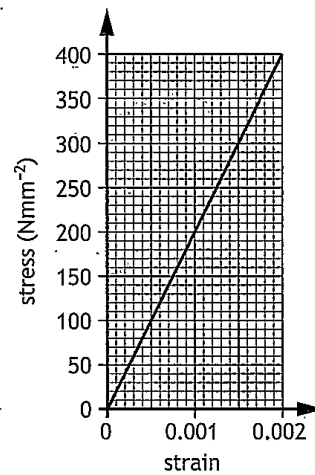


Figure 2



MARKS

1. (continued)

- (a) (i) State the name of the range 0 to A. 1

elastic range

- (ii) State the name of the range A to D. 1

plastic range

- (b) (i) Calculate, using the information from Figure 2, Young's Modulus for this material. 1

$$\begin{aligned} E &= \frac{\sigma}{\epsilon} \\ &= \frac{400}{0.002} \\ &= 200 \times 10^3 \text{ N mm}^{-2} \\ &= 200 \text{ kN mm}^{-2} \\ &= \end{aligned}$$

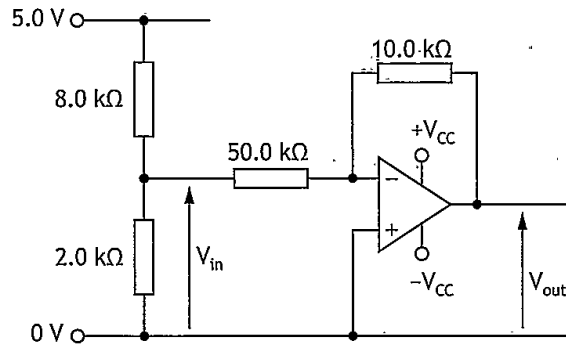
- (ii) State the property identified by point C on Figure 1. 1

maximum load

[Turn over]

MARKS

2. Part of an electronic circuit is shown.



(a) Calculate  $V_{out}$ .

2

$$V_{in} = \frac{2}{10} \times 5$$

$$= \underline{1V}$$

$$V_o = -\frac{10}{50} \times 1$$

$$= \underline{-0.2V}$$

(b) Describe how the gain of this op-amp circuit could be decreased.

1

increasing the value of  $R_f$ .

After testing, it was decided to add an additional op-amp configuration to change the polarity of  $V_{out}$ .

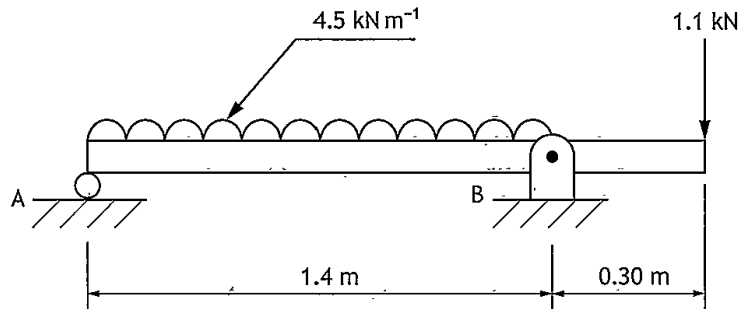
(c) State the name of the op-amp configuration required to perform this task.

1

inverting

MARKS

3. A beam used in the construction of a covered walkway is shown.



Calculate by taking moments about B, the vertical reaction at A.

3

$$4.5 \times 1.4 = \underline{6.3 \text{ kN}}$$

~~$$1.4A = (6.3 \times 0.7) + (1.1 \times 0.3)$$~~

~~$$1.4A = 4.74$$~~
~~$$A = 3.39 \text{ kN}$$~~

$$1.4A + (1.1 \times 0.3) = (6.3 \times 0.7)$$

$$A = \underline{2.9 \text{ kN}}$$

MARKS

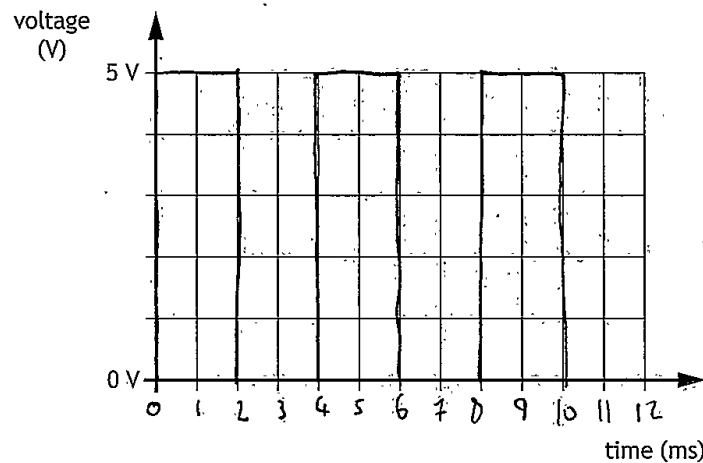
4. The speed at which an automatic garage door opens is controlled by a motor using pulse-width modulation (PWM).



- (a) Complete the graph below to show how PWM could be used to make the motor rotate at half speed.

You should include at least three pulses.

2



- (b) Describe how the speed of this motor could be decreased using PWM.

1

By increasing the space time (gaps in between pulses) or by decreasing the mark time (time of pulses).

MARKS

## 4. (continued)

An alternative method of speed control involves varying the size of the DC voltage supplied to the motor.

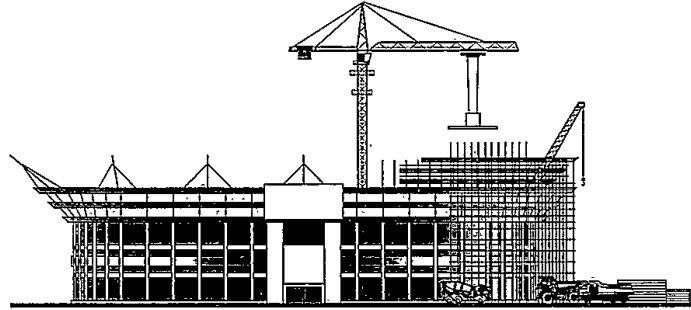
- (c) Describe one advantage of using PWM in comparison to varying the size of the voltage supply. 1

It is easier to vary the size of the pulses.  
Suddenly changing the size of DC Voltage can  
cause damage, the PWM allows 'soft start'.

[Turn over

MARKS

5. The capacity of a sports stadium is being increased. This needs an additional stand to be built on top of the existing structure.



A structural engineer is involved in the design of this new structure.

Describe two examples of how the structural engineer will use their knowledge of materials in the design of the new structure.

2

Example 1 It is a Sports Stadium so the risk to human life is high if anything fails. The structural engineer will know what materials to select to ensure the highest factor of safety needed.

Example 2 The structural engineer will also have knowledge of the stresses different materials can withstand before reacting. They can use this to help figure out the factor of safety. The structural engineer will need to estimate the load put on the materials by the people in the stadium. The structural engineer will also need to analyse the old stand to ensure it can withstand a new one on top of it and potentially where it needs to be reinforced.

MARKS

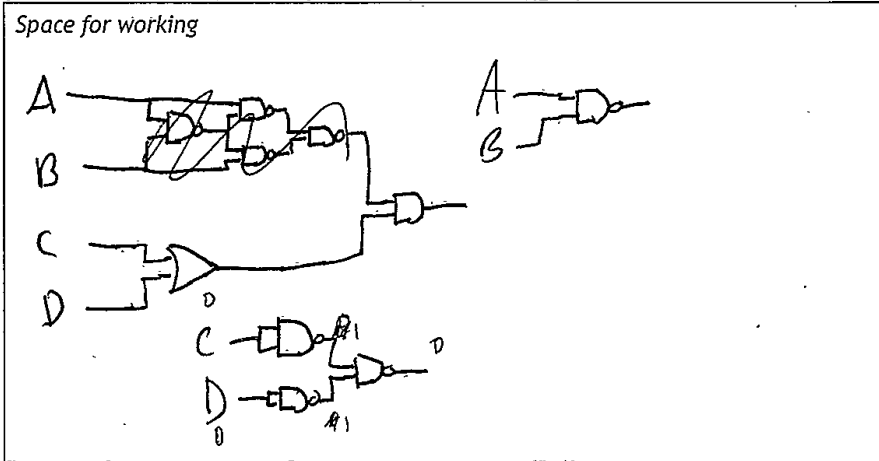
6. An electronic engineer has designed a combinational logic circuit according to the Boolean equation, shown below.

$$Z = (\overline{A \cdot B}) \cdot (C + D)$$

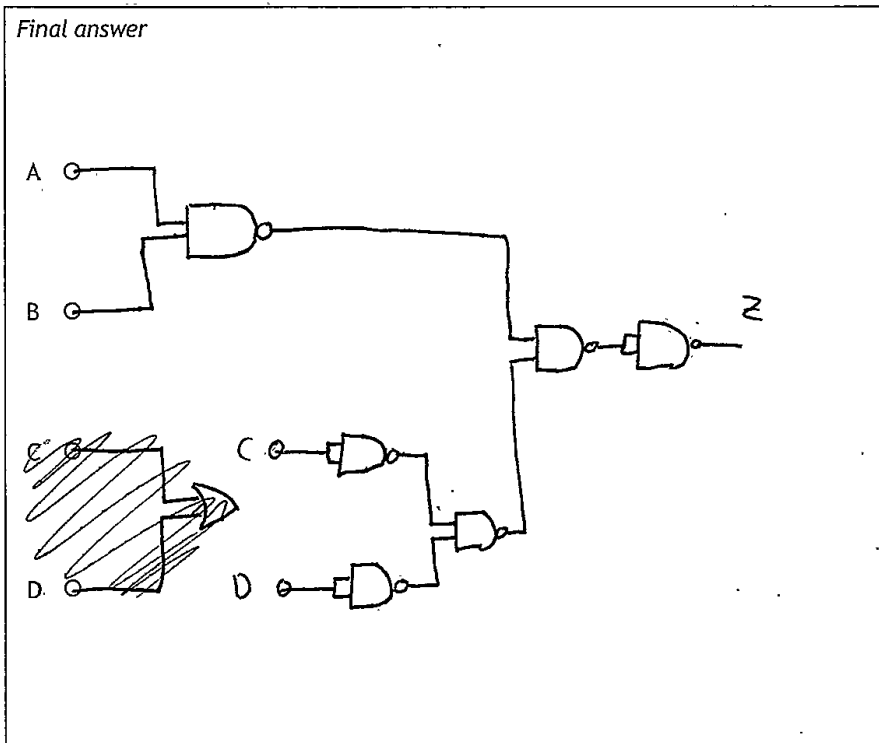
Draw a NAND equivalent circuit for this Boolean equation.

3

Space for working



Final answer



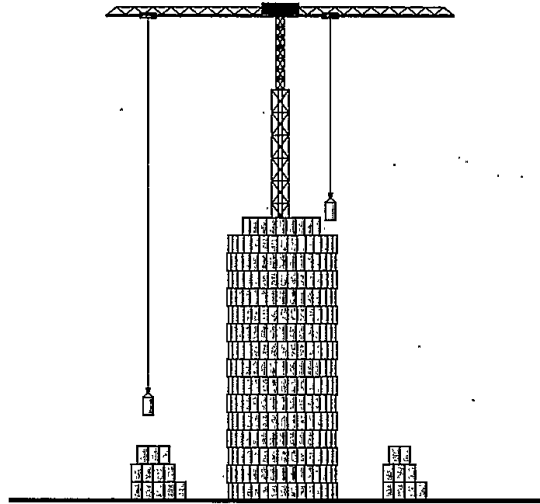


MARKS

## SECTION 2 — 90 marks

Attempt ALL questions

7. An engineering team has produced a prototype system to store excess energy from power plants.



When electricity production exceeds demand, electric motors are used to lift concrete blocks and place them in 'towers'. When the blocks are returned to ground level electricity is reclaimed by generators.

The first block has a mass of 10,000.0 kg. The system that raises this block is 92% efficient.

- (a) Calculate the energy required to raise this block 32 m.

2

$$\begin{aligned}
 E &= mgh \\
 &= 10,000 \times 9.8 \times 32 \\
 &= 3136 \text{ kJ} \times 1.08 \\
 &= 3387 \text{ kJ} \\
 &= 3390 \text{ kJ} \\
 &= 3.39 \times 10^6 \text{ kJ}
 \end{aligned}$$

MARKS

## 7. (continued)

A second block applies a force of 80.0 kN to the supporting wire rope.

As this block is returned to ground level (at constant speed) its supporting wire rope turns a generator and electricity is reclaimed. This part of the system is 87% efficient.

- (b) Calculate the power output from the generator if this block descends 15 m in 11 seconds.

3

$$\begin{aligned}
 P &= \frac{e}{t} & e &= mgh \\
 &= \frac{130 \times 10^6}{11} & &= (80 \times 10^3 \times 9.8) \times 9.8 \times 15 \\
 &= \underline{\underline{11.8 \text{ MW}}} & &= 115 \times 10^6 \text{ J} \\
 & & &= 115 \times 1.013 \\
 & & &= \underline{\underline{130 \times 10^6 \text{ J}}}
 \end{aligned}$$

The wire rope holding the 80.0 kN block as it is lifted is made from mild steel and has a diameter of 48 mm.

- (c) Calculate the factor of safety in the wire rope when it raises this block at a steady speed.

4

$$\begin{aligned}
 \text{F.O.S.} &= \frac{430}{44.2} & \sigma &= \frac{80 \times 10^3}{\pi \times (48 \times 10^{-3})^2} \\
 &= \underline{\underline{9.73}} & &= \frac{80000}{\pi \times 0.002304} \\
 & & &= \frac{80000}{0.00725} \\
 & & &= \underline{\underline{44.2}}
 \end{aligned}$$

## 7. (continued)

MARKS

- (d) Describe two economic and two environmental impacts that this system would have.

4

Economic impact 1 This could have an impact on the local jobs as this machine could replace people's jobs and leave them unemployed. This would have a negative impact on the local economy.

Economic impact 2 This could have a positive impact on the local economy as if excess energy can be used then ~~there will be~~ it will be cheaper in the times it is needed this could help people by lowering their energy bills.

Environmental impact 1 This is good for the environment as it is more efficient and is a way to potentially store renewable energy.

Environmental impact 2 This could have a negative impact on the local environment as many trucks and heavy machinery would be in the area, disturbing wildlife and causing pollution.

- (e) Describe two advantages that this system has over a chemical battery storage system for excess electrical energy.

2

Advantage 1 Batteries need to be disposed of once used so it will be cheaper for the company if they don't need to have to spend money properly disposing batteries.

Advantage 2 It is better for the environment as used batteries can cause harm to nature due to the chemicals inside of them, which can leak out.

8. An anti-lock braking system is used to control the speed of an elevator as it descends. This uses a form of pulse-width modulation operated by a microcontroller.

If the speed of the elevator is too fast, the brakes will increase the proportion of operating time.

The table below identifies the connections to the microcontroller.

Input	Pin	Output
	7	brake
ground level sensor	1	
speed sensor (analogue)	0	

The system must perform the following steps.

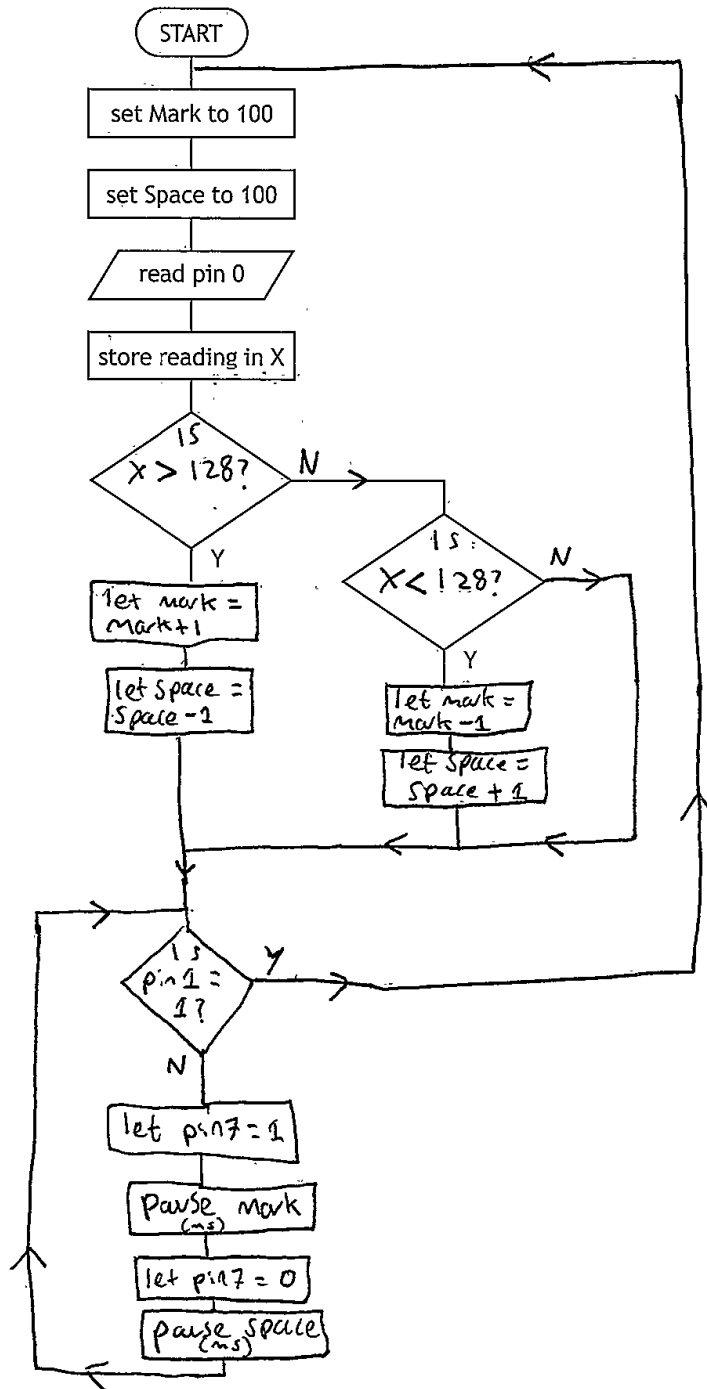
- Values for **mark** and **space** both need to be initially set to a value of 100
- A reading must be taken from a speed sensor and its value stored in variable X
- If the value of X is greater than 128 then **mark** increases by 1 and **space** decreases by 1
- If the value of X is smaller than 128 then **mark** decreases by 1 and **space** increases by 1
- If the value of X is 128 then **mark** and **space** do not change
- The brake must be switched on and off for the times specified **mark** and **space** (this will be in milliseconds)
- The process must continue until the ground level sensor is activated

MARKS

8. (continued)

(a) Complete, with reference to the specification and the input/output table, this flow chart for the control of the system.

8



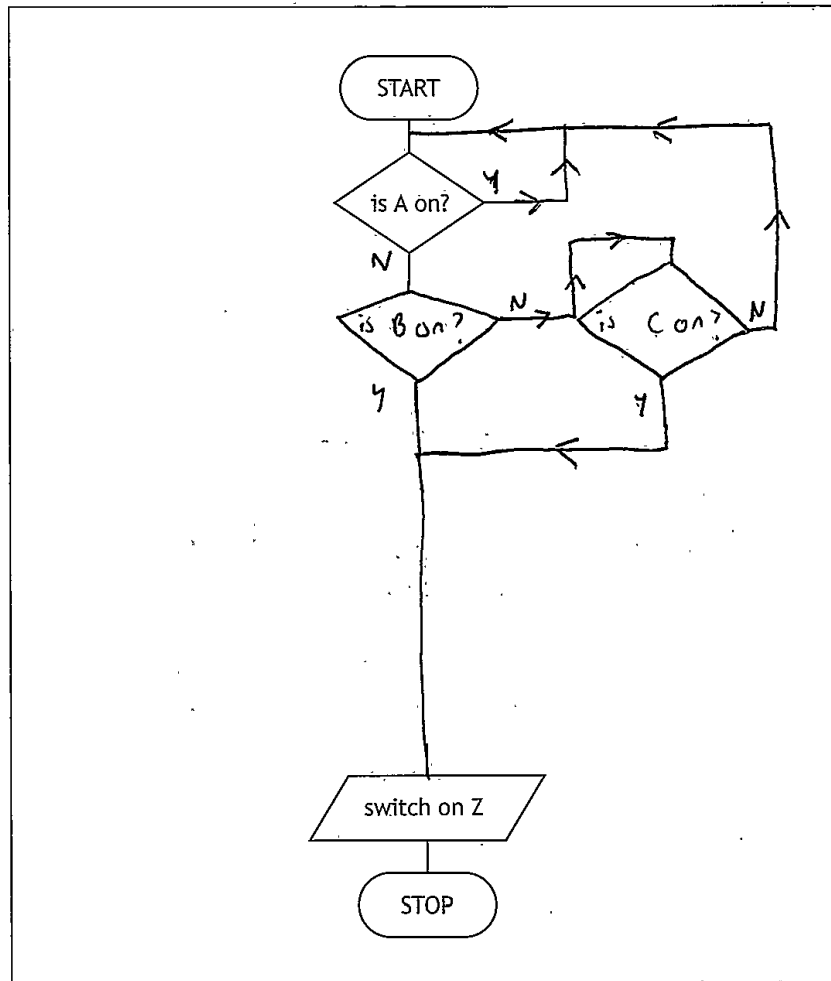
MARKS

8. (continued)

An alarm (Z) is part of the elevator's operating system and needs to be activated under the conditions given by the following Boolean equation.

$$Z = \bar{A} \cdot (B + C)$$

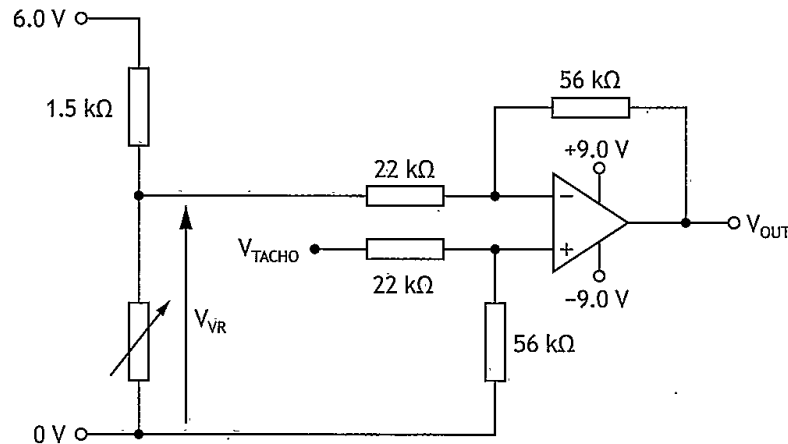
(b) Complete the following flowchart to perform the function described above. 3



MARKS

## 8. (continued)

An alternative system to control the force applied by the brake is also tested. As the speed of the elevator varies from a reference value the output of the circuit changes proportionately. The speed of the elevator is monitored by a tachogenerator.



When testing the circuit, the voltage from the tachogenerator ( $V_{TACHO}$ ) was found to be 2.3 V.

- (c) (i) Calculate the resistance of the variable resistor in the circuit shown above when the output voltage of the op-amp is +4.5 V.

4

$$V_i = \frac{R_2}{1.5 \times 10^3 + R_2} \times 6$$

$$V_o = \frac{R_f}{R_i} (V_2 - V_1)$$

$$4.5 = \frac{56}{22} \times (2.3 - V_i)$$

$$V_i = 0.53 \text{ V}$$

$$0.53 = \frac{R_2}{1.5 \times 10^3 + R_2} \times 6$$

$$0.088... = \frac{R_2}{1.5 \times 10^3 + R_2}$$

$$133 + 0.088... R_2 = R_2$$

$$\frac{133}{R_2} = 1 - 0.088...$$

$$\frac{133}{0.911...} = R_2$$

$$R_2 = 146 \Omega$$

MARKS

8. (c) (continued)

- (ii) Describe, with reference to the circuit, how the reference speed of the elevator could be increased.

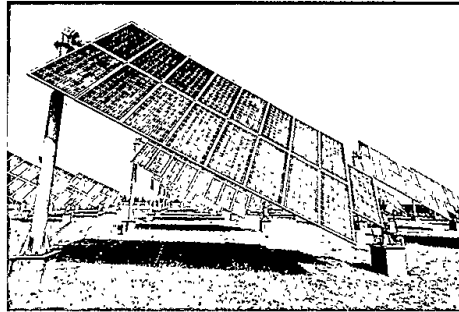
1

By increasing the value of  $R_f$  or  
decreasing the value of  $R_i$ .

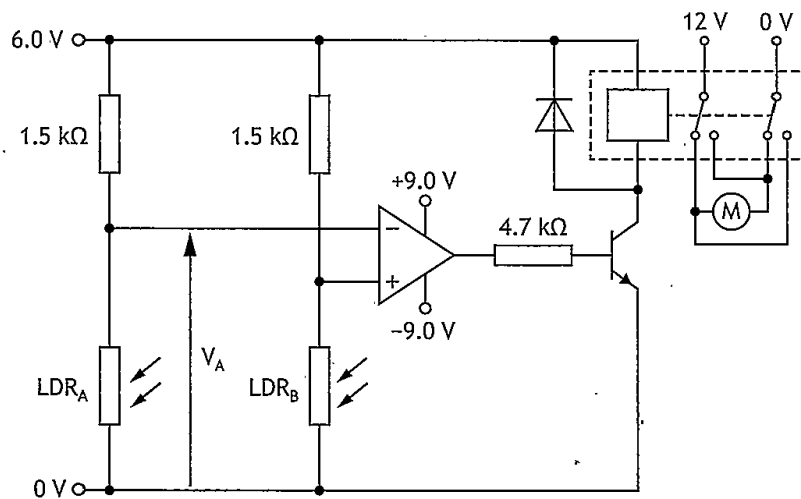
[Turn over



9. A system is needed to alter the position of a solar panel so that it is constantly facing the sun during daylight hours. If one sensor gives a higher reading than the other, a motor will turn the panel in the brighter direction.



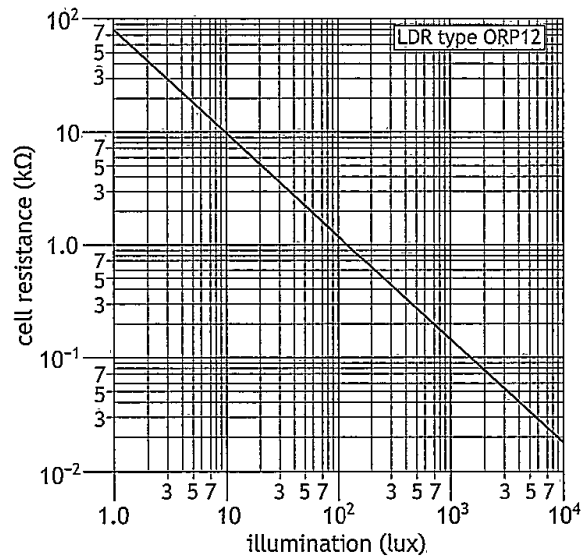
A preliminary design of the control circuit is shown below.



MARKS

## 9. (continued)

The characteristics of the LDRs are shown in the graph below.



- (a) Calculate  $V_A$  if the light level on  $LDR_A$  is 20 lux.

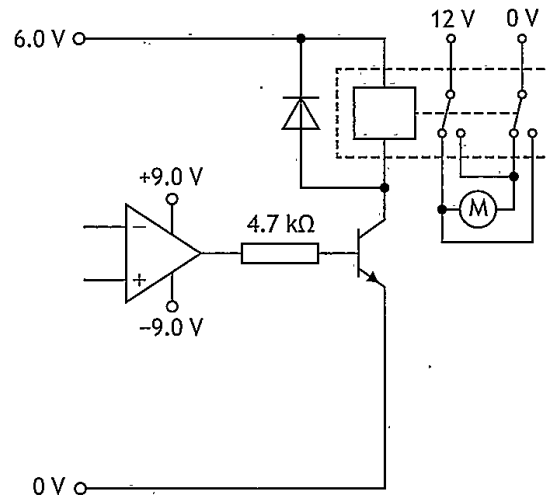
2

$$\begin{aligned}
 & \underline{5k\Omega} \\
 & V_A = \frac{5}{1.5 + 5} \times 6 \\
 & \quad \quad \quad \underline{6} \\
 & = 4.6V \\
 & \quad \quad \quad \underline{=}
 \end{aligned}$$

MARKS

## 9. (continued)

Part of the control circuit is shown below.



- (b) (i) Calculate the base current to the transistor when the op-amp saturates positively.  
Assume  $V_{be}$  is 0.70 V. The op-amp output saturates at 75% of the supply voltage.

3

$$\begin{aligned}
 6 \times 0.75 &= 4.5 \text{ V} \\
 4.5 + 0.7 &= 5.2 \text{ V} \\
 V &= IR \\
 I_b &= \frac{5.2}{4.7 \times 10^3} \\
 &= 1.11 \text{ mA}
 \end{aligned}$$

MARKS

## 9. (b) (continued)

The relay has a resistance of  $5.0 \Omega$ .

- (ii) Calculate the minimum current gain of the transistor to ensure it is fully saturated when the op-amp is saturated positively.

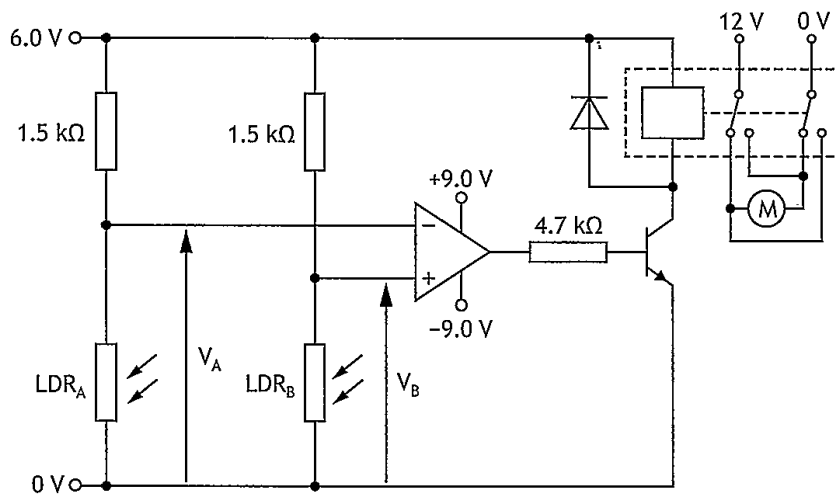
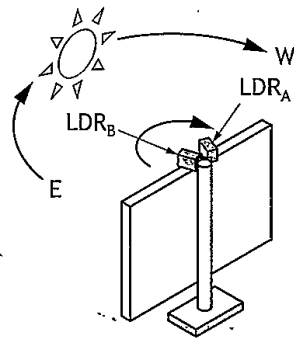
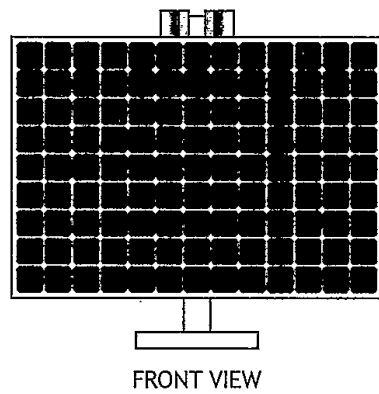
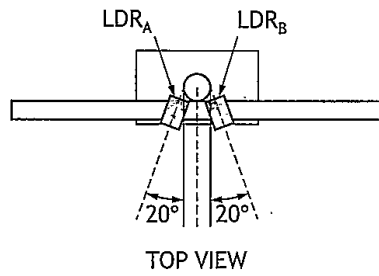
2

$$h_{FE} = \frac{I_C}{I_B}$$
$$= \frac{1.2}{1.11 \times 10^{-3}}$$
$$= \underline{\underline{1081}}$$
$$I_C = \frac{V}{R}$$
$$= \frac{6}{5}$$
$$= \underline{\underline{1.2 A}}$$

[Turn over

9. (continued)

While testing the circuit,  $V_A$  was found to be less than  $V_B$  and the motor rotated, moving the solar panel towards the sun's position.



MARKS

## 9. (continued)

- (c) Describe, referring to the circuit on the opposite page, what will happen as the solar panel moves.

Your answer must refer to the input voltage dividers, the op-amp and transistor, and the relay and motor.

6

Input voltage dividers If it moves west, LDRA will increase, this will reduce the value for  $V_A$ .  
If it moves east however, LDRE will increase this will reduce the value for  $V_B$ .  
The higher the light level, the smaller the value for  $V_A/V_B$ .

Op-amp and transistor If it moves west  $V_A < V_B$  so it will saturate the op-amp will saturate positively.  
If it moves east,  $V_A > V_B$  so the op-amp will saturate negatively.

Relay and motor Based on whether the op-amp will saturate positively or negatively the direction of the motor will change.  
If the light level is higher the output voltage from the op-amp will be lower, ~~sketching~~ reducing how fast the motor turns, to keep it in the sun.

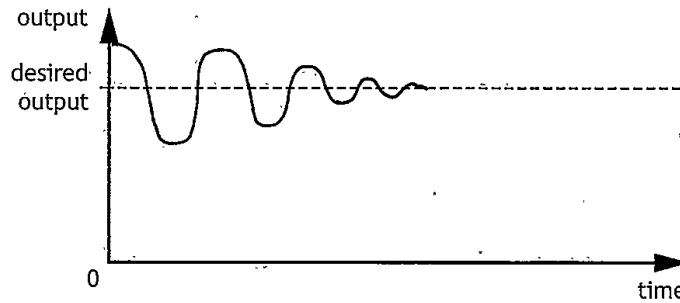
[Turn over

MARKS

## 9. (continued)

The op-amp control circuit uses two-state control.

- (d) (i) Complete the graph below to show how the output of a two-state control system changes as it approaches the desired output. 2



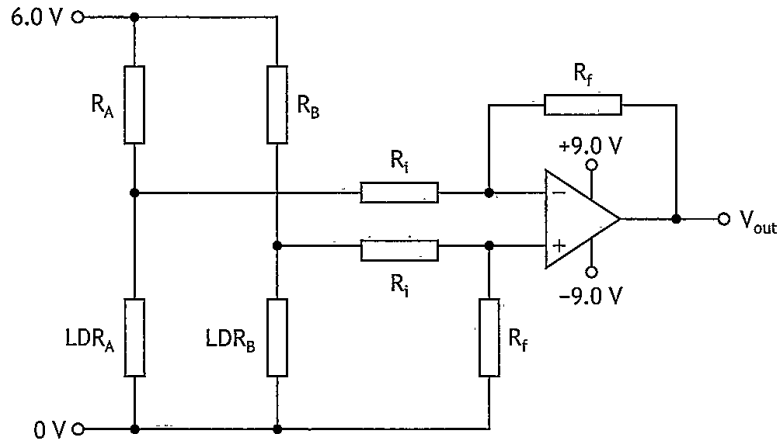
- (ii) Describe the impact that this type of control would have on the mechanical output of the system. 1

The panels would be moving east to west before stabilising.

MARKS

9. (continued)

An alternative control circuit is also tested.



- (e) (i) State the type of control produced by this type of circuit. 1
- Two State
- 
- (ii) Describe the difference between the control produced by this circuit and a two-state control system. You can use diagrams or graphs to illustrate your answer. 3

[Turn over



MARKS

10. An engineering team is experimenting with different control systems to operate a number of pneumatic cylinders. The following truth table shows the conditions under which one of the cylinders must outstroke.

A	B	C	D	Z
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

- (a) Write a Boolean equation for the output Z.

2

$$Z = C \cdot (\bar{D} + (A \cdot B))$$

A—  
B—  
C—  
D—

$$C \cdot (\bar{D} + (A \cdot B))$$

MARKS

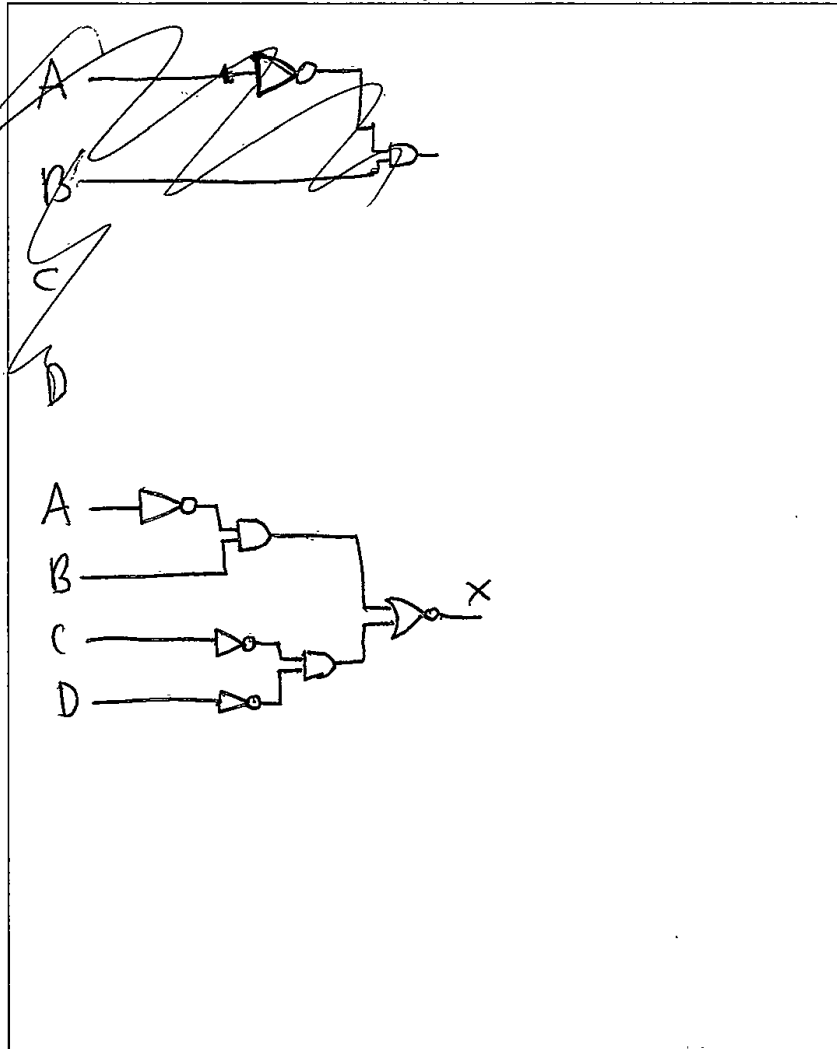
10. (continued)

A second cylinder operates under the following conditions.

$$X = \bar{A} \cdot B \oplus (\bar{C} \cdot D)$$

(b) Draw a logic diagram to perform this function.

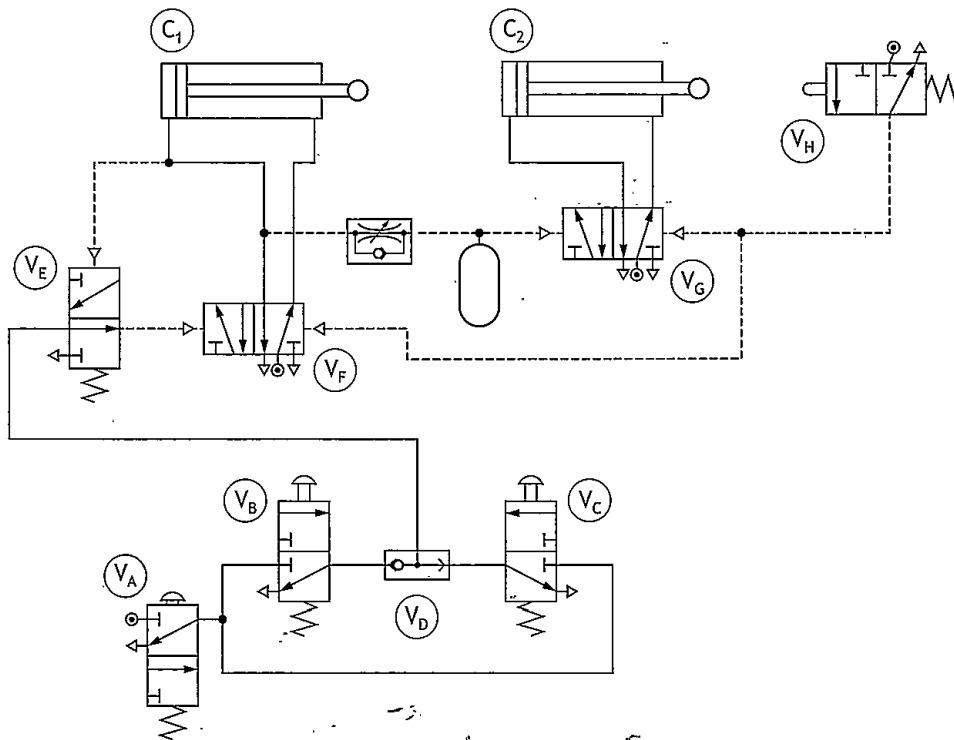
4



[Turn over

10. (continued)

Two further cylinders are to be controlled by the following circuit.



MARKS

## 10. (continued)

- (c) (i) Describe the operation of this circuit, highlighting the function of each component and the conditions that will cause the cylinders to instroke and outstroke.

6

When  $V_A$ ... is pressed and  $V_B$  or  $V_C$ , the pilot air passes through  $V_D$  and towards  $V_E$ . This sends pilot air to  $V_F$  which will outstroke  $C_1$ .

The pilot air also travels through a time delay to activate  $V_G$ . This will outstroke  $C_2$ , pushing the button at  $V_H$ , activating it. This will send pilot air back to  $V_A$ , but due to the buttons,  $V_A$ ,  $V_B$  and  $V_C$  being all spring loaded no conflict will occur. This will instroke  $C_2$ . The air will also go to  $V_F$  when will cause  $C_1$  to instroke, ~~at the start~~

~~$V_B$  and  $V_C$  are pressed, a conflict will occur and the system will occur at  $V_D$ .~~ If at the start both  $V_A$ ,  $V_B$  and  $V_C$  are pressed, conflict will occur at  $V_D$ .

The engineering team are considering changing the circuit shown opposite to one that is operated by a microcontroller.

- (ii) Describe two reasons why using a microcontroller-based system is preferred to a fully pneumatic system.

2

Micro-adjustments can be made rather than just on or off.

Saves compressed air can be dangerous.

If cylinders are only used to be halfway activated.

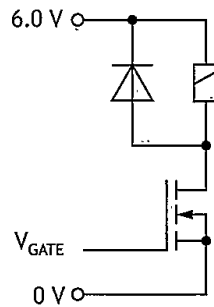
More reliable, less chance of problems occurring from air leaking or other issues.

Saves

MARKS

## 10. (continued)

In order to use a microcontroller-based system, solenoid valves need to be used. The following circuit has been designed to actuate one of the solenoids.



The solenoid is rated 12 W at 6.0 V. The MOSFET has a resistance of 0.70  $\Omega$  when switched on.

- (d) (i) Calculate the resistance of the solenoid.

1

$$P = \frac{V^2}{R}$$

$$R = \frac{6^2}{12}$$

$$= 3 \Omega$$

- (ii) Calculate the current through the MOSFET when it is fully switched on.

1

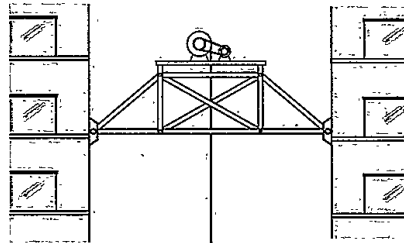
$$V = IR$$

$$I = \frac{6}{0.7}$$

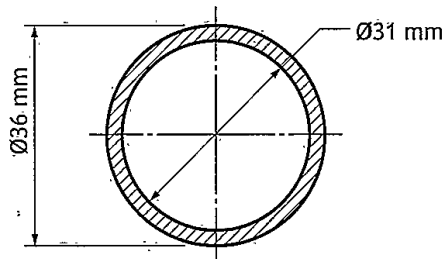
$$= 8.6 \text{ A}$$

MARKS

11. During a construction project in a city centre location, a lifting platform is installed between two high rise buildings.



One of the members in the structure has a cross-section as shown below, with an internal diameter of 31 mm, and an external diameter of 36 mm.



This mild steel member has a strain of  $4.6 \times 10^{-5}$  when subjected to a load.

- (a) Calculate the load carried by this member.

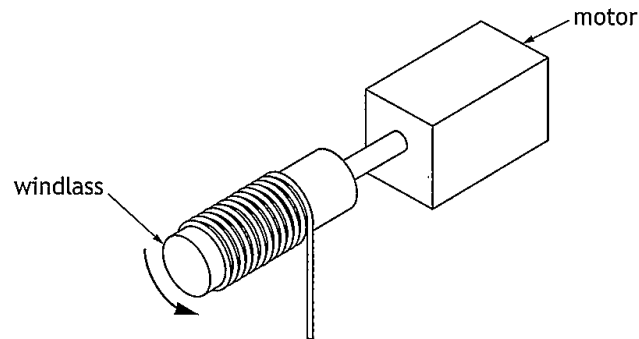
4

$$\begin{aligned}
 E &= 196 \\
 \epsilon &= \frac{\sigma}{E} & \sigma &= \frac{F}{A} & A_E &= \pi r^2 \\
 & & & & &= \pi \times 36^2 \\
 & & & & &= 1296\pi \\
 \sigma &= 4.6 \times 10^{-5} \times 196 \times 10^3 \\
 &= 9.016 \text{ kN/m}^2 & A_{\text{steel}} &= \pi r^2 \\
 & & &= \pi \times 31^2 \\
 & & &= 961\pi \\
 F &= 9.016 \times 10^3 \times 335\pi \\
 &= 9.5 \text{ kN} & &= 1296\pi - 961\pi \\
 & & &= 335\pi \text{ mm}^2 \\
 F &= 9.016 \times 335\pi \\
 &= 9.5 \text{ kN}
 \end{aligned}$$

MARKS

## 11. (continued)

A motor-driven winch system is used for lifting construction materials with up to 12,000 kg of mass. The windlass, with 320 mm diameter, rotates at 12 revolutions per minute.



(b) Calculate the mechanical power required by this motor.

5

$$P = 2\pi nT$$

$$T = Fr$$

$$= (12,000 \times 9.8) \times (160 \times 10^{-3})$$

$$= 18.8 \text{ kNm}$$

$$P = 2\pi \times 0.2 \times 18.8 \times 10^3$$

$$= 23.6 \text{ kW}$$

=

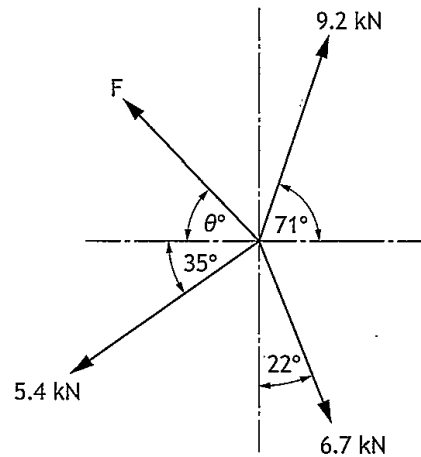
$$\frac{12}{60} = 0.2 \text{ revs}^{-1}$$

MARKS

## 11. (continued)

Later in the construction project, the lifting platform supports cables used to suspend a concrete beam above the site until it is ready for positioning.

The diagram below represents the concurrent force system while the beam is in suspension.



- (c) Calculate the magnitude and angle of the force  $F$ , required to maintain equilibrium.

6

$$9.2 \times \sin 71 + F \sin \theta = 5.4 \sin 35 + 6.7 \cos 22$$

$$9.2 \times \cos 71 + 6.7 \times \sin 22 = 5.4 \times \cos 35 + F \cos \theta$$

~~$F \sin \theta = 1.07$~~

$$F \cos \theta = 1.08$$

$$F \sin \theta = 0.61$$

$$\frac{F \sin \theta}{F \cos \theta} = \frac{0.61}{1.08}$$

$$\tan \theta = 0.56$$

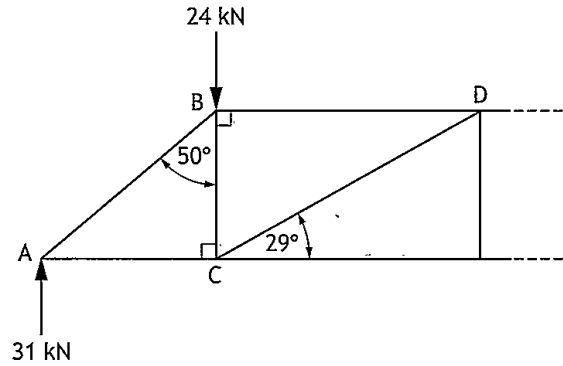
$$\theta = 29^\circ$$

$$F = \frac{0.61}{\cos 29} \quad F = \underline{\underline{1.24 \text{ kN}}}$$



MARKS

12. The free-body diagram for part of a structure and its loading is shown below.



Calculate, using nodal analysis, the magnitude and nature of forces in members AB, AC, BC, BD and CD.

Show all working and final units on the page opposite.

Complete the table below.

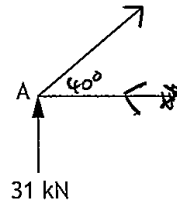
8

Member	Magnitude	Nature
AB	48 kN	strut
AC	37 kN	tie
BC	55 kN	tie
BD	37 kN	strut
CD	113 kN	strut

12. (continued)

Space for working

node A



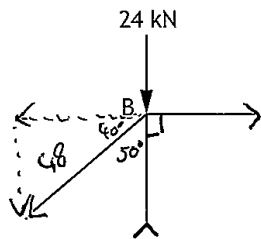
$$AB \sin 40 = 31$$

$$AB = \underline{48 \text{ kN}}$$

$$AC = AB \cos 40$$

$$= \underline{37 \text{ kN}}$$

node B



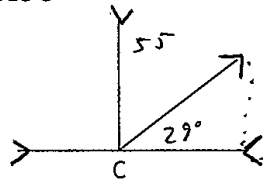
$$24 + 48 \sin 40 = BC$$

$$BC = \underline{55 \text{ kN}}$$

$$48 \times \cos 40 = BD$$

$$BD = \underline{37 \text{ kN}}$$

node C



$$CD \sin 29 = 55$$

$$CD = \underline{113 \text{ kN}}$$

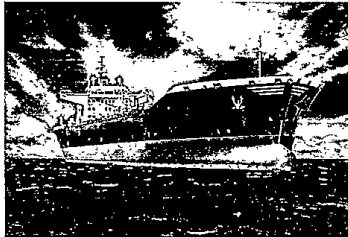
[END OF QUESTION PAPER]

# Candidate 2 evidence

**SECTION 1 — 20 marks**

Attempt ALL questions

1. A new material is being tested for use in the manufacture of ships.



The results of a tensile test on the material are shown in Figure 1.

The range of 0 to A is shown magnified in Figure 2.

Figure 1

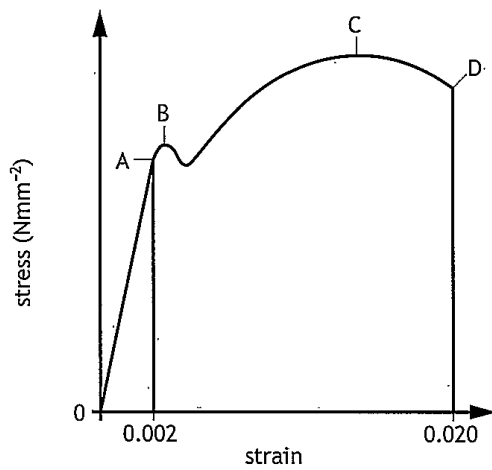
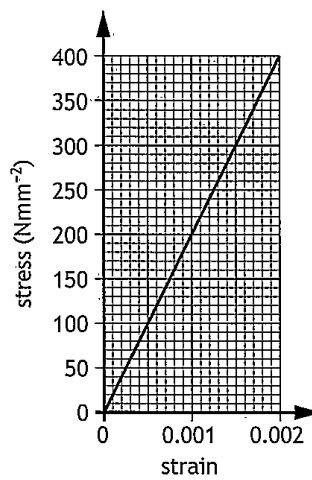


Figure 2



MARKS

1. (continued)

- (a) (i) State the name of the range 0 to A. 1

Yield

- (ii) State the name of the range A to D. 1

- (b) (i) Calculate, using the information from Figure 2, Young's Modulus for this material. 1

$$E = \frac{\sigma}{\epsilon}$$

$$E = \frac{400}{0.002}$$

$$E = \underline{\underline{200,000 \text{ N/mm}^2}}$$

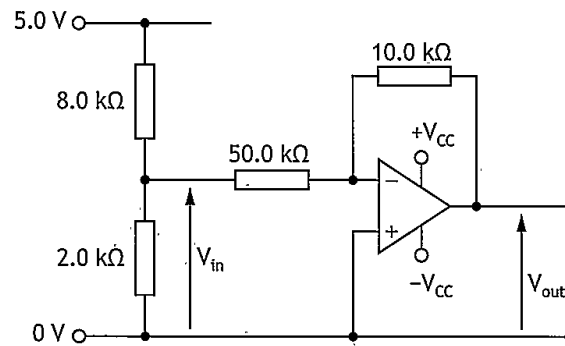
- (ii) State the property identified by point C on Figure 1. 1

Ultimate Stress

[Turn over

MARKS

2. Part of an electronic circuit is shown.



(a) Calculate  $V_{out}$ .

2

$$V_o = -\frac{R_f}{R_i} \times v_i$$

$$V_o = -\frac{10}{50} \times 5$$

$$V_o = \underline{\underline{-1V}}$$

(b) Describe how the gain of this op-amp circuit could be decreased.

1

By increasing the resistance

After testing, it was decided to add an additional op-amp configuration to change the polarity of  $V_{out}$ .

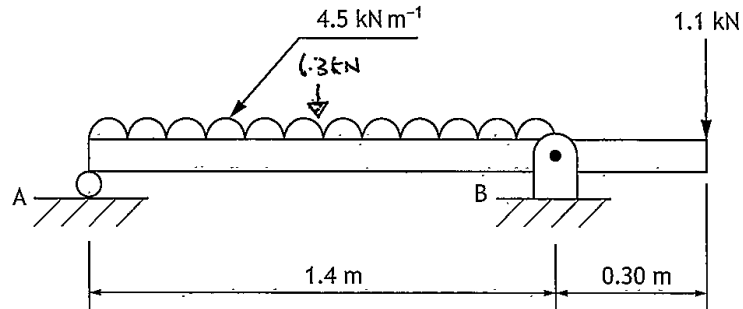
(c) State the name of the op-amp configuration required to perform this task.

1

Inverting op-amp

MARKS

3. A beam used in the construction of a covered walkway is shown.



Calculate by taking moments about B, the vertical reaction at A.

3

$$\begin{aligned} \sum \text{CWM} &= \sum \text{ACWM} && 4.5 \times 1.4 = 6.3 \text{ kN} \\ (1.1 \times 0.3) &= (6.3 \times 0.7) R_B \\ 4.41 R_B &= 0.33 \\ R_B &= \frac{0.33}{4.41} \\ R_B &= 0.07 \text{ kN} \end{aligned}$$

MARKS

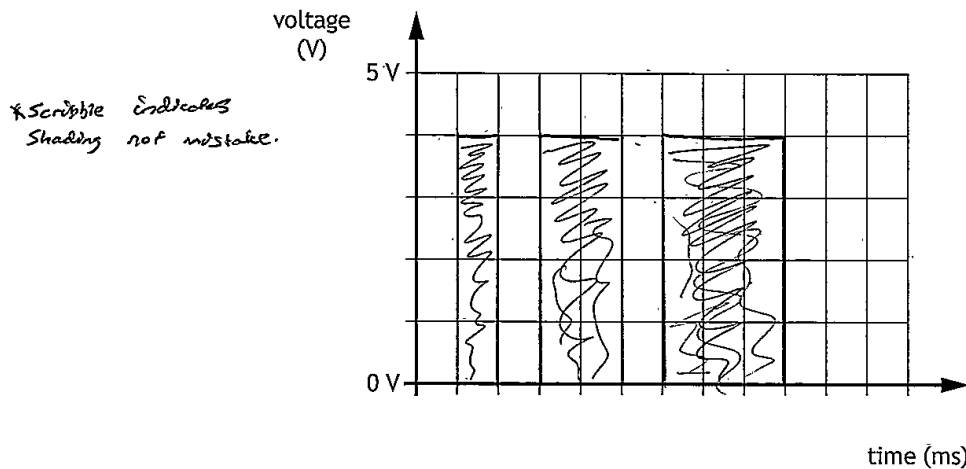
4. The speed at which an automatic garage door opens is controlled by a motor using pulse-width modulation (PWM).



- (a) Complete the graph below to show how PWM could be used to make the motor rotate at half speed.

You should include at least three pulses.

2



- (b) Describe how the speed of this motor could be decreased using PWM.

1

The speed of the motor could be decreased using PWM by decreasing the voltage.

---



---

MARKS

## 4. (continued)

An alternative method of speed control involves varying the size of the DC voltage supplied to the motor.

- (c) Describe one advantage of using PWM in comparison to varying the size of the voltage supply.

1

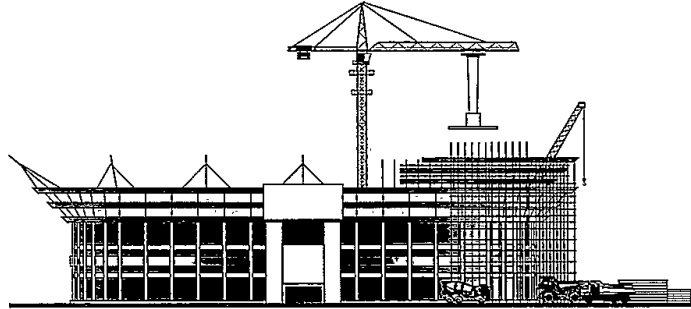
With a PWM you don't have to constantly  
replace it. meanwhile with varying the size you  
have to constantly replace the size of the voltage  
supply.

[Turn over



MARK:

5. The capacity of a sports stadium is being increased. This needs an additional stand to be built on top of the existing structure.



A structural engineer is involved in the design of this new structure.

Describe two examples of how the structural engineer will use their knowledge of materials in the design of the new structure.

2

Example 1 The structural engineer would calculate  
the forces acting on the materials so that  
it wouldn't collapse under pressure.

Example 2 The structural engineer would analyse the  
properties of the materials to see if it  
would withstand the natural elements.

MARKS

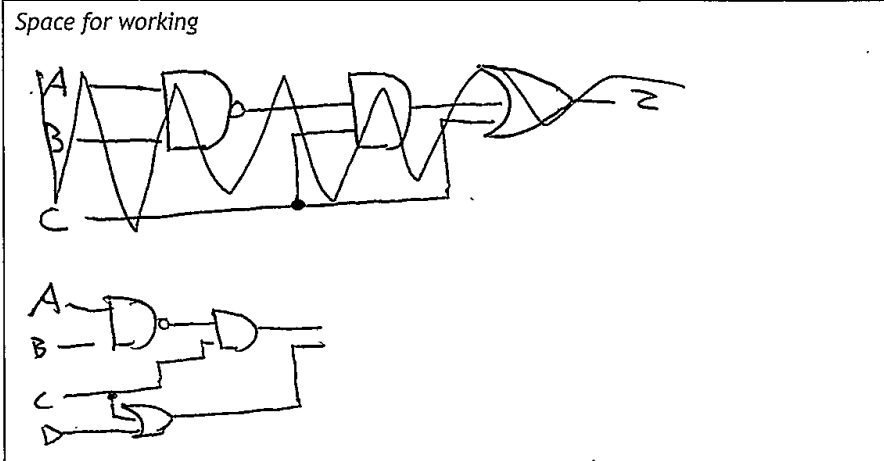
6. An electronic engineer has designed a combinational logic circuit according to the Boolean equation, shown below.

$$Z = (\overline{A \cdot B}) \cdot (C + D)$$

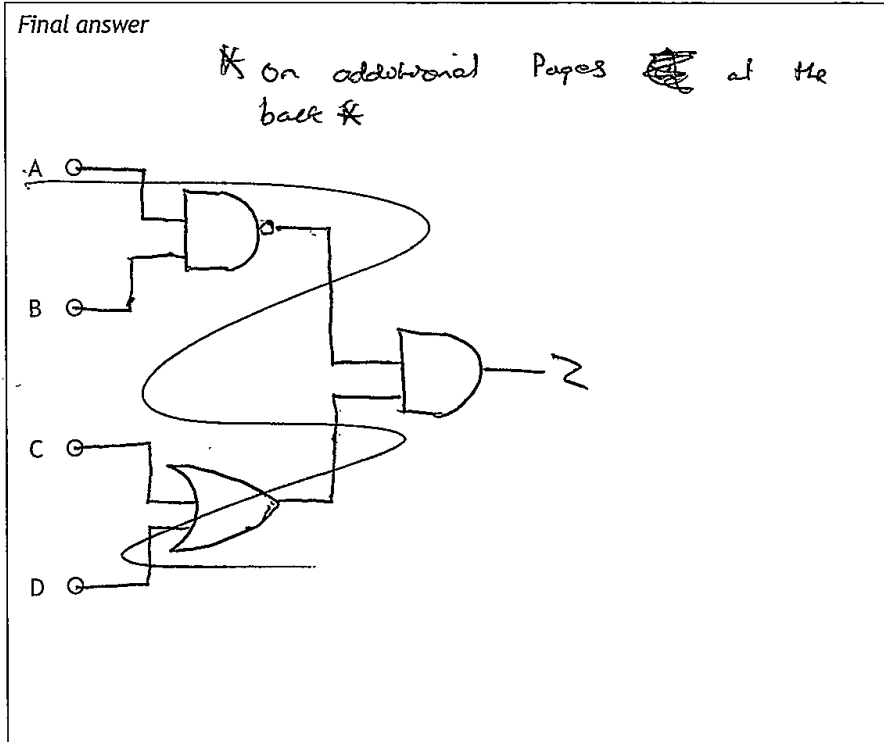
Draw a NAND equivalent circuit for this Boolean equation.

3

Space for working



Final answer

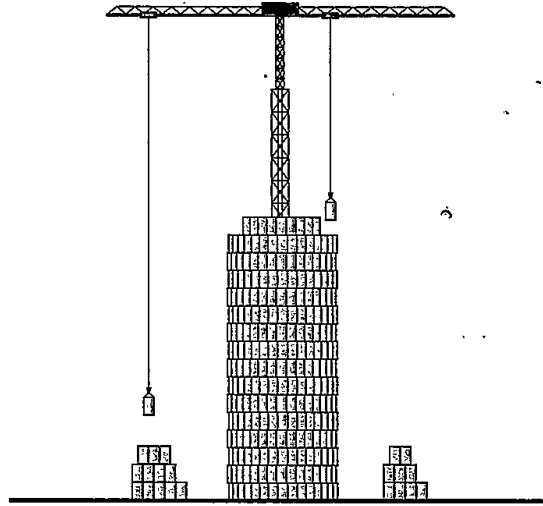


MARKS

## SECTION 2 — 90 marks

Attempt ALL questions

7. An engineering team has produced a prototype system to store excess energy from power plants.



When electricity production exceeds demand, electric motors are used to lift concrete blocks and place them in 'towers'. When the blocks are returned to ground level electricity is reclaimed by generators.

The first block has a mass of 10,000.0 kg. The system that raises this block is 92% efficient.

- (a) Calculate the energy required to raise this block 32 m.

2

$$E_p = m g h$$
$$E_p = 10,000 \times 9.8 \times 32$$
$$E_p = 3136000 \text{ J}$$
$$0.92 \times 3136000 = \underline{\underline{2885120 \text{ J}}}$$

MARKS

## 7. (continued)

A second block applies a force of 80.0 kN to the supporting wire-rope.

As this block is returned to ground level (at constant speed) its supporting wire rope turns a generator and electricity is reclaimed. This part of the system is 87% efficient.

- (b) Calculate the power output from the generator if this block descends 15 m in 11 seconds.

3

$$\eta = \frac{\text{Power out}}{\text{Power in}}$$

$$P = \frac{E}{t} \quad 0.87 = \frac{285090}{262283}$$

$$P = \frac{285090}{11} \quad \text{\& on additional pages}$$

$$P = 25909.090$$

$$P = 25909.090 \text{ W}$$

$$P = 262283 \text{ W}$$

The wire rope holding the 80.0 kN block as it is lifted is made from mild steel and has a diameter of 48 mm.

- (c) Calculate the factor of safety in the wire rope when it raises this block at a steady speed.

4

$$FOS = \frac{US}{ms}$$

$$FOS = \frac{430}{1.6}$$

$$FOS = 268.75$$

$$FOS = \underline{\underline{270}}$$

$$\sigma = \frac{F}{A}$$

$$\sigma = \frac{80,000}{\frac{\pi \cdot 48^2}{4}}$$

$$\sigma = 1.6 \text{ Nmm}^{-2}$$

7. (continued)

MARKS

- (d) Describe two economic and two environmental impacts that this system would have.

4

Economic impact 1 It would provide job opportunities for people to earn money for their families etc...

Economic impact 2 The system is cheaper to store. Since storing chemical batteries are more expensive to keep safe.

Environmental impact 1 It's a 'cleaner' way to store energy since they're not being stored inside the power plants.

Environmental impact 2 Nearby residents No habitats would be ruined if there was a leak since some habitats may be affected by pollution by making the electrical energy from power plants.

- (e) Describe two advantages that this system has over a chemical battery storage system for excess electrical energy.

2

Advantage 1 If there is a leak, chemicals won't spill meaning it's safer.

Advantage 2 Electrical energy is safer better for the environment to store rather than storing chemical batteries.

8. An anti-lock braking system is used to control the speed of an elevator as it descends. This uses a form of pulse-width modulation operated by a microcontroller.

If the speed of the elevator is too fast, the brakes will increase the proportion of operating time.

The table below identifies the connections to the microcontroller.

Input	Pin	Output
	7	brake
ground level sensor	1	
speed sensor (analogue)	0	

The system must perform the following steps.

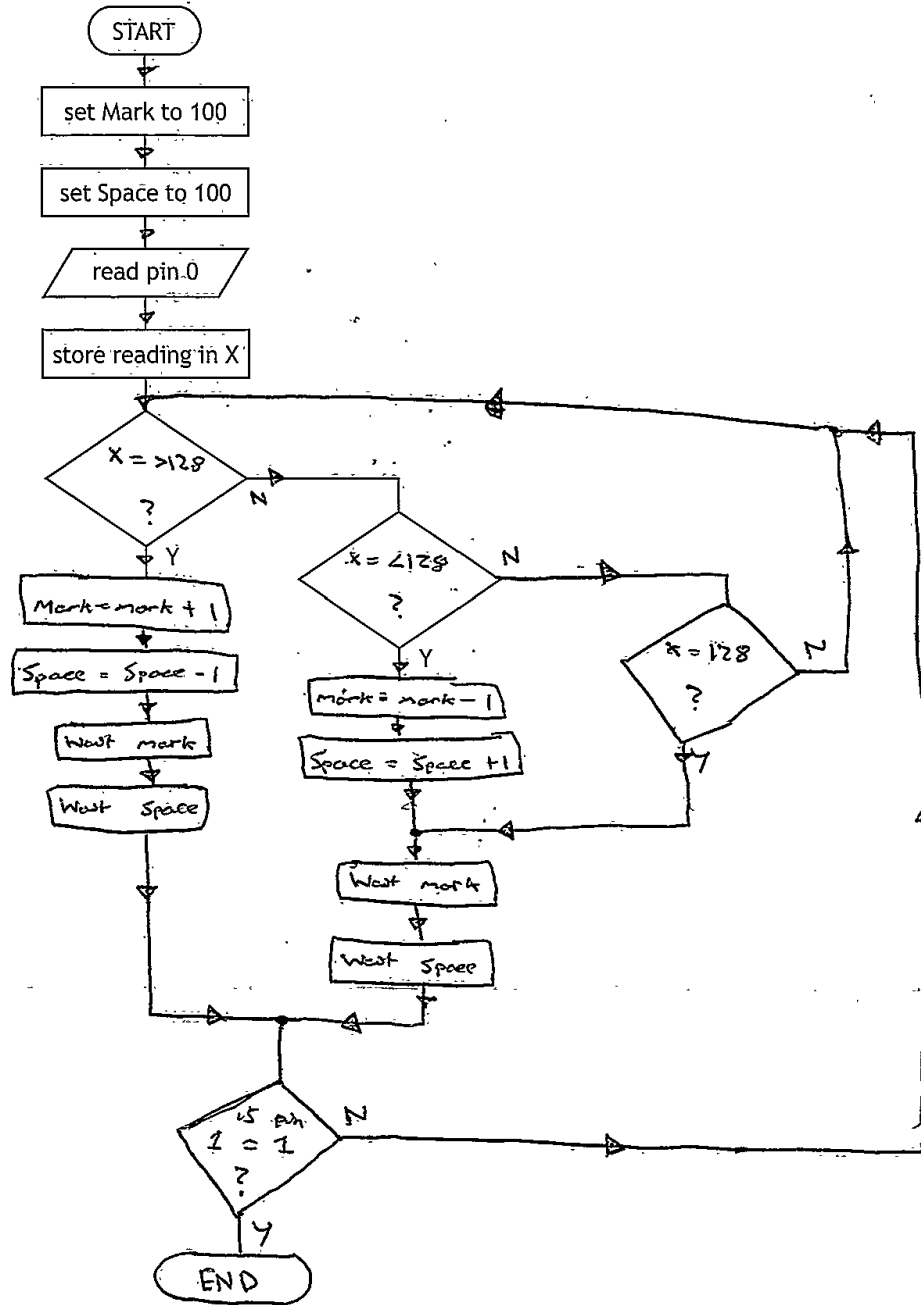
- Values for **mark** and **space** both need to be initially set to a value of 100
- A reading must be taken from a speed sensor and its value stored in variable X
- If the value of X is greater than 128 then **mark** increases by 1 and **space** decreases by 1
- If the value of X is smaller than 128 then **mark** decreases by 1 and **space** increases by 1
- If the value of X is 128 then **mark** and **space** do not change
- The brake must be switched on and off for the times specified **mark** and **space** (this will be in milliseconds)
- The process must continue until the ground level sensor is activated

MARKS

8. (continued)

(a) Complete, with reference to the specification and the input/output table, this flow chart for the control of the system.

8



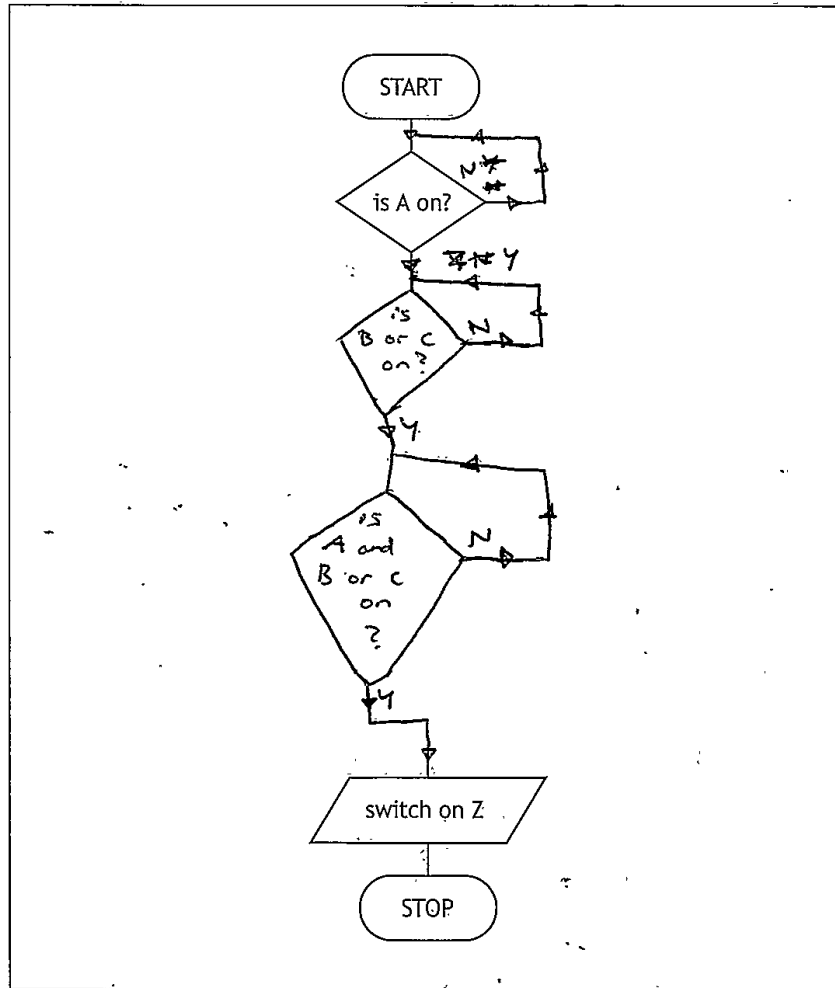
MARKS

8. (continued)

An alarm (Z) is part of the elevator's operating system and needs to be activated under the conditions given by the following Boolean equation.

$$Z = \bar{A} \cdot (B + C)$$

(b) Complete the following flowchart to perform the function described above. 3

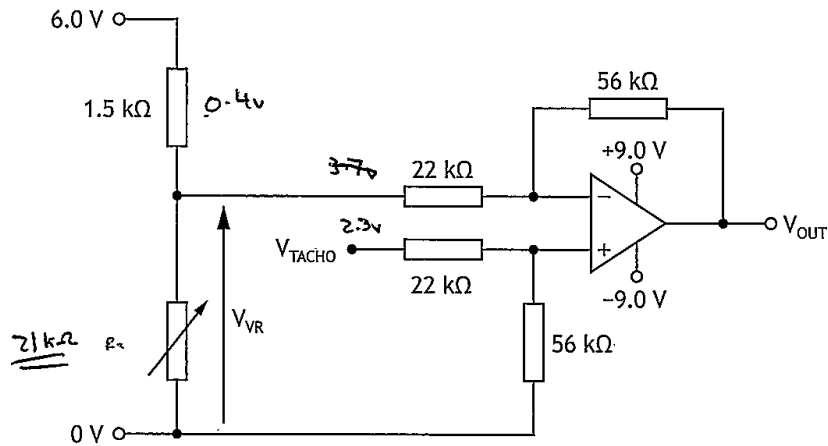




MARKS

8. (continued)

An alternative system to control the force applied by the brake is also tested. As the speed of the elevator varies from a reference value the output of the circuit changes proportionately. The speed of the elevator is monitored by a tachogenerator.



When testing the circuit, the voltage from the tachogenerator ( $V_{TACHO}$ ) was found to be 2.3 V.

- (c) (i) Calculate the resistance of the variable resistor in the circuit shown above when the output voltage of the op-amp is +4.5 V.

4

$V = \frac{R_2}{R_1} \times V_2$   $6 - 2.3 = 3.7V$  \* next page \*

$V_0 = \frac{R_f}{R_i} (V_2 - V_1)$  →

$4.5 = \frac{56}{22} \times (2.3 - V_1)$

$= 4.5 \times 22$

MARKS

8. (c) (continued)

- (ii) Describe, with reference to the circuit, how the reference speed of the elevator could be increased.

1

The speed could be increased by decreasing the resistor values. So that more current can flow.

[Turn over

Q8 (b):

$$V_o = \frac{R_F}{R_i} (V_2 - V_1)$$

$$4.5 = \frac{56}{22} \times (2.3 - V_1)$$

~~$$V_1 = \frac{56}{22} \times \left( \frac{2.3 - 4.5}{4.5 - 2.3} \right)$$~~

$$V_{VR} = \frac{56}{22} \times (2.3 - 4.5)$$

$$V_{VR} = -5.6V$$

$$\frac{V_1}{V_2} = \frac{R_1}{R_2}$$

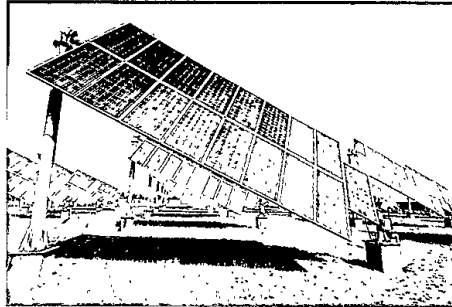
$$\frac{0.4}{5.6} = \frac{1.5}{R_2}$$

$$0.4 R_2 = 1.5 \times 5.6$$

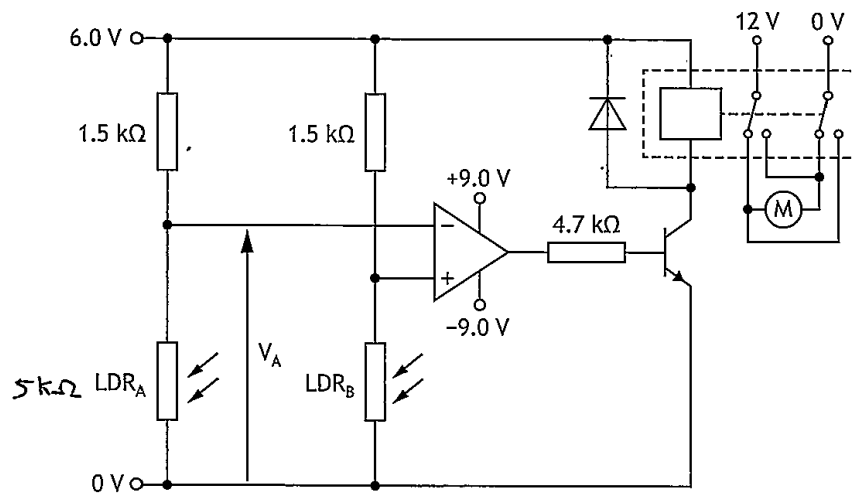
$$R_2 = \frac{1.5 \times 5.6}{0.4}$$

$$R_2 = \underline{\underline{21 \text{ k}\Omega}}$$

9. A system is needed to alter the position of a solar panel so that it is constantly facing the sun during daylight hours. If one sensor gives a higher reading than the other, a motor will turn the panel in the brighter direction.



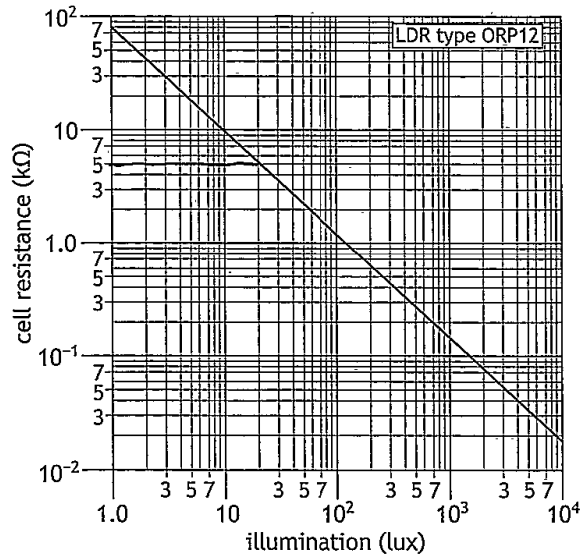
A preliminary design of the control circuit is shown below.



MARKS

9. (continued)

The characteristics of the LDRs are shown in the graph below.



(a) Calculate  $V_A$  if the light level on  $LDR_A$  is 20 lux.

2

Handwritten student work for part (a):

20 lux = 5000  $\Omega$

~~$V_A = \frac{R_2}{R_T} \times V_S$~~

$V_A = \frac{5}{1.5} \times 6$

$V_A = 20V$

$V_A = \frac{R_2}{R_T} \times V_S$

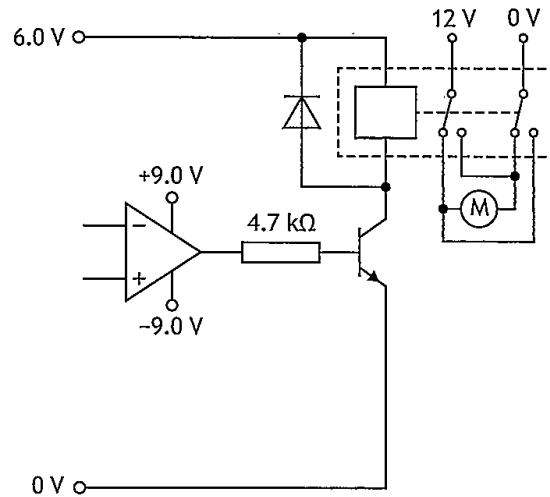
$V_A = \frac{5}{6.5} \times 6$

$V_A = \underline{\underline{4.62V}}$

MARKS

9. (continued)

Part of the control circuit is shown below.



- (b) (i) Calculate the base current to the transistor when the op-amp saturates positively.  
 Assume  $V_{be}$  is 0.70 V. The op-amp output saturates at 75% of the supply voltage.

3

$6 - 0.7 = 5.3V$   
 $0.75 \times 5.3 = 3.98V$   
 ~~$V = IR$~~   
 ~~$3.98 = I \times 4700$~~   
 ~~$4700I = 3.98$~~   
 ~~$I = \frac{3.98}{4700}$~~   
 ~~$I = 0.00085A$~~   
 $V = IR$   
 $3.98 = I \times 4.7$   
 $I = \frac{3.98}{4.7}$   
 $I = 0.85A$

MARKS

9. (b) (continued)

The relay has a resistance of  $5.0 \Omega$ .

(ii) Calculate the minimum current gain of the transistor to ensure it is fully saturated when the op-amp is saturated positively.

2

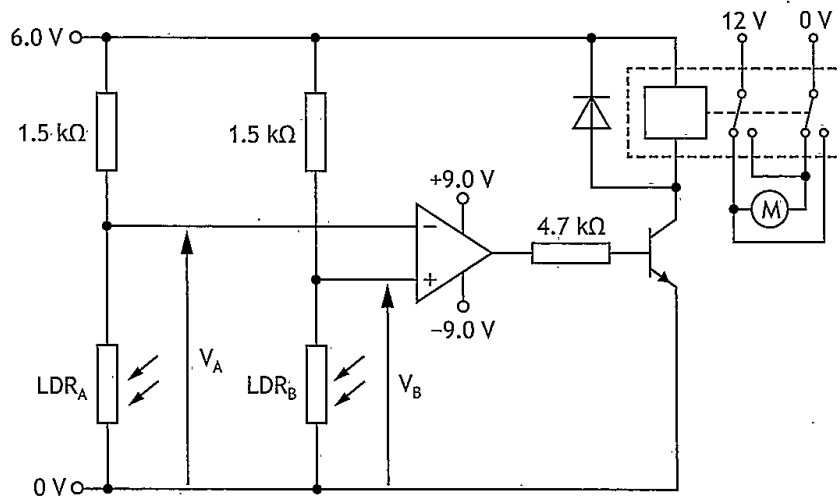
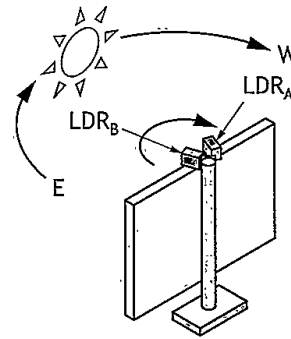
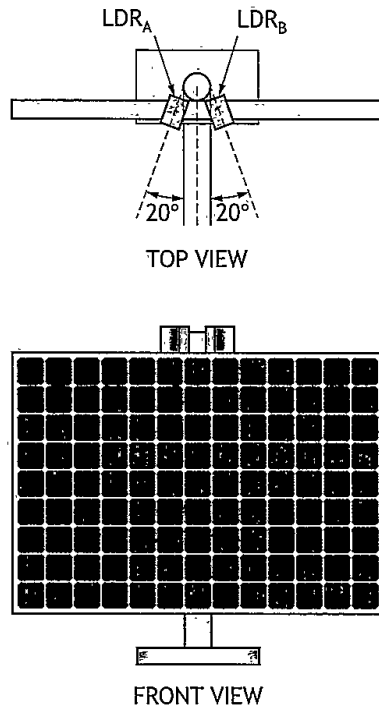
$$\begin{aligned}
 V &= I R \\
 5.3 &= I \times 5 \\
 I &= \frac{5.3}{5} \\
 I_c &= 1.06 \text{ A} \\
 h_{fe} &= \frac{I_c}{I_b} \\
 h_{fe} &= \frac{1.06}{0.85} \\
 h_{fe} &= \underline{\underline{1.25}}
 \end{aligned}$$

$$\begin{aligned}
 h_{fe} &= \frac{I_c}{I_b} \\
 h_{fe} &= \frac{1.06}{0.0085} \\
 h_{fe} &= 1247
 \end{aligned}$$

[Turn over

9. (continued)

While testing the circuit,  $V_A$  was found to be less than  $V_B$  and the motor rotated, moving the solar panel towards the sun's position.



MARKS

## 9. (continued)

- (c) Describe, referring to the circuit on the opposite page, what will happen as the solar panel moves.

Your answer must refer to the input voltage dividers, the op-amp and transistor, and the relay and motor.

6

Input voltage dividers When light level drops <sup>In LDR</sup> resistance  
~~increases~~ and voltage increases which results  
in the voltage to be higher than LDR  
Since LDR's light level increases so resistance  
and voltage for LDR is low.

Op-amp and transistor Since LDR's voltage is higher  
than LDR's that means that the op-amp  
will saturate positively resulting in the transistor  
to switch on as the voltage is above 0.7V.  
The resistor protects the transistor from too much  
current.

Relay and motor Since the transistor is on that  
means that the relay switches on which causes  
it to change state which causes the 12V to  
flow to the motor switching it on. The  
diode protects the relay from back E.M.F.

[Turn over

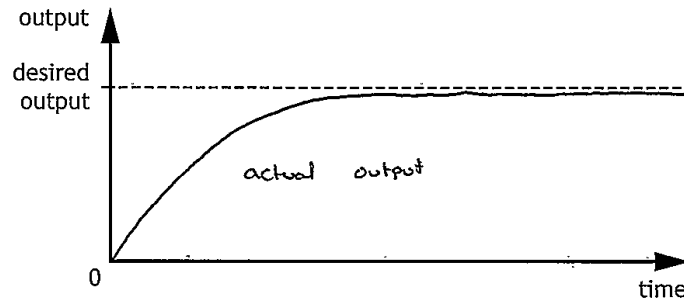


MARKS

## 9. (continued)

The op-amp control circuit uses two-state control.

- (d) (i) Complete the graph below to show how the output of a two-state control system changes as it approaches the desired output. 2



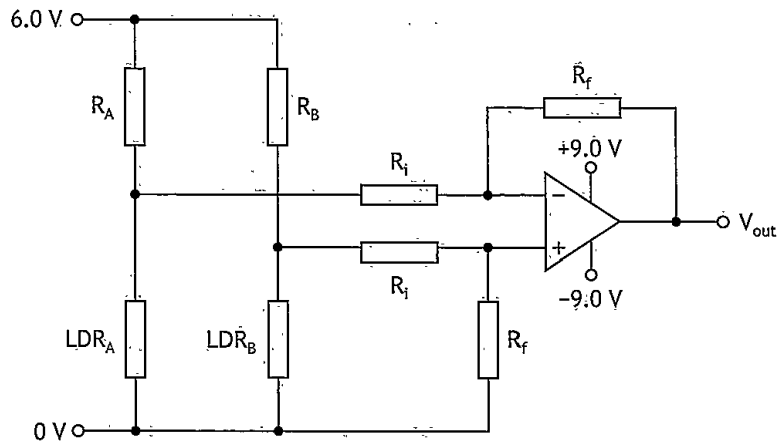
- (ii) Describe the impact that this type of control would have on the mechanical output of the system. 1

This would cause the mechanical output  
to ~~lag~~ never reach the desired out put.  
\_\_\_\_\_

MARKS

9. (continued)

An alternative control circuit is also tested.



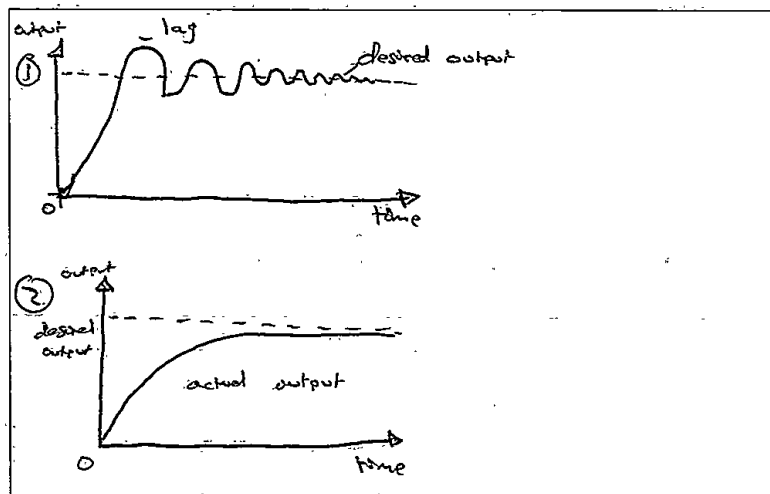
- (e) (i) State the type of control produced by this type of circuit.

1

Proportional

- (ii) Describe the difference between the control produced by this circuit and a two-state control system. You can use diagrams or graphs to illustrate your answer.

3



[Turn over

MARKS

10. An engineering team is experimenting with different control systems to operate a number of pneumatic cylinders. The following truth table shows the conditions under which one of the cylinders must outstroke.

A	B	C	D	Z
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

 $\bar{A}.B.\bar{C}.D$ 

- (a) Write a Boolean equation for the output Z.

2

$$Z = (\bar{A}.B.\bar{C}.D) + (\bar{A}.\bar{B}.\bar{C}.D) + (\bar{A}.\bar{B}.C.\bar{D})$$

MARKS

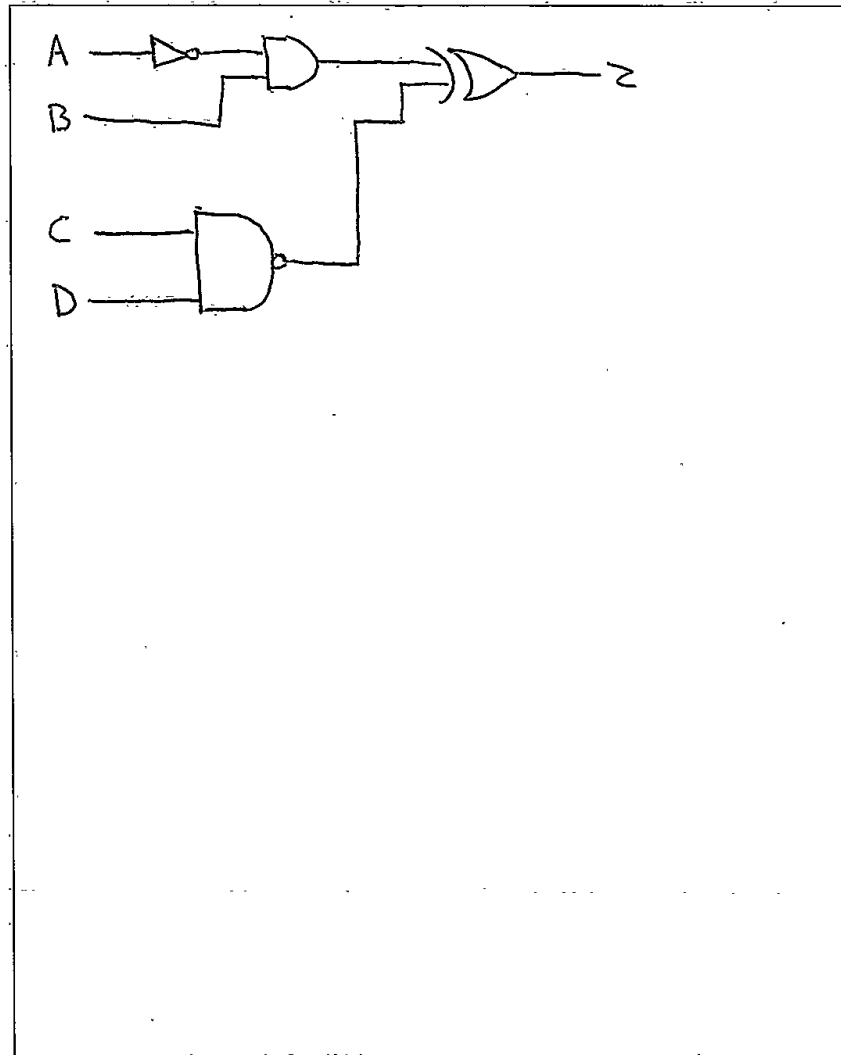
10. (continued)

A second cylinder operates under the following conditions.

$$X = \bar{A} \cdot B \oplus (\bar{C} \cdot D)$$

(b) Draw a logic diagram to perform this function.

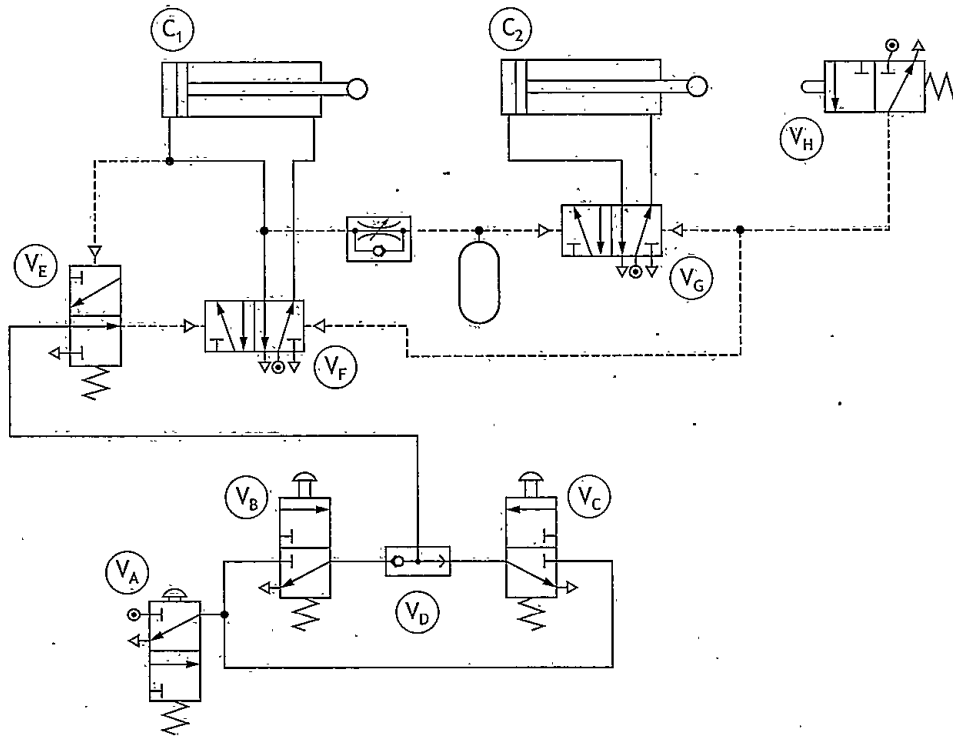
4



[Turn over

10. (continued)

Two further cylinders are to be controlled by the following circuit.



MARKS

## 10. (continued)

- (c) (i) Describe the operation of this circuit, highlighting the function of each component and the conditions that will cause the cylinders to instroke and outstroke.

6

When  $V_A$ ... is pressed mains air and either  
 $V_B$  or  $V_C$  is pressed mains air flows to  
 $V_E$  and into  $V_F$  causing  $C_1$  to outstroke.  
 meanwhile <sup>pilot</sup> air flows to the uni-directional restrictor  
 and reservoir causing a time delay and  
 into  $V_G$ , this causes  $C_2$  to outstroke which  
 activates  $V_H$  causing pilot air to flow to  
 $V_G$  causing  $C_2$  to instroke meanwhile pilot air  
 flows down to  $V_F$  which causes  $C_1$  to instroke.  
 air inside  $C_1$  gets pushed back and changes  
 to pilot air which flows to  $V_F$  which cuts  
 off the mains air supply from  $V_B$  or  $V_C$ . This  
 causes the system to reset.

The engineering team are considering changing the circuit shown opposite to one that is operated by a microcontroller.

- (ii) Describe two reasons why using a microcontroller-based system is preferred to a fully pneumatic system.

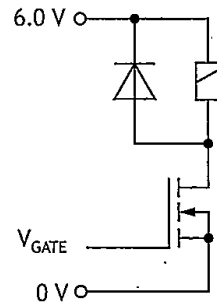
2

A microcontroller is very small and compact  
 meaning that you don't need to spend a lot  
 of money on the components. It's also easy  
 to repair since all you have to do is re-programme  
 rather than replacing the parts (components).

MARKS

## 10. (continued)

In order to use a microcontroller-based system, solenoid valves need to be used. The following circuit has been designed to actuate one of the solenoids.



The solenoid is rated 12 W at 6.0 V. The MOSFET has a resistance of 0.70 Ω when switched on.

- (d) (i) Calculate the resistance of the solenoid.

1

$$P = \frac{V^2}{R}$$

$$\frac{12}{1} = \frac{6^2}{R}$$

$$R = \frac{6^2}{12}$$

$$R = \underline{\underline{3 \Omega}}$$

- (ii) Calculate the current through the MOSFET when it is fully switched on.

1

$$V = I R$$

$$6 = I \times 0.70$$

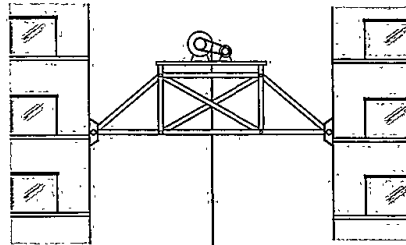
$$0.70 I = 6$$

$$I = \frac{6}{0.70}$$

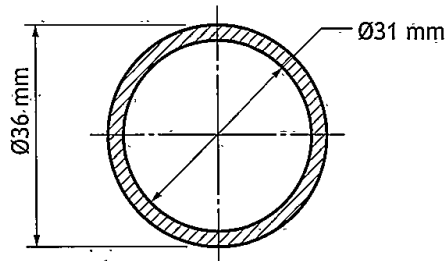
$$I = \underline{\underline{8.6 A}}$$

MARKS

11. During a construction project in a city centre location, a lifting-platform is installed between two high-rise buildings.



One of the members in the structure has a cross-section as shown below, with an internal diameter of 31 mm, and an external diameter of 36 mm.



This mild steel member has a strain of  $4.6 \times 10^{-5}$  when subjected to a load.

- (a) Calculate the load carried by this member.

4

$$A_1 = \frac{\pi d^2}{4}$$

$$A_1 = \frac{\pi \times 31^2}{4}$$

$$A_1 = 754.77 \text{ mm}^2$$

$$A_2 = \frac{\pi d^2}{4}$$

$$A_2 = \frac{\pi \times 36^2}{4}$$

$$A_2 = 1017.88 \text{ mm}^2$$

$$A_T = A_2 - A_1$$

$$A_T = 1017.88 - 754.77$$

$$A_T = 263.11 \text{ mm}^2$$

$$\sigma = \frac{F}{A}$$

$$\frac{4.6 \times 10^{-5}}{1} = \frac{F}{263.11}$$

$$F = 4.6 \times 10^{-5} \times 263.11$$

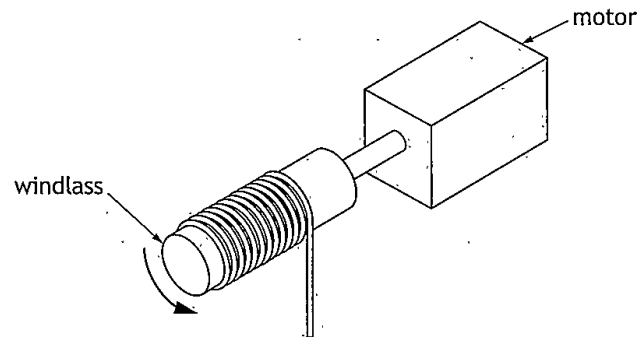
$$F = 0.012 \text{ N}$$



MARKS

11. (continued)

A motor-driven winch system is used for lifting construction materials with up to 12,000 kg of mass. The windlass, with 320 mm diameter, rotates at 12 revolutions per minute.



(b) Calculate the mechanical power required by this motor.

5

$$12 \div 60 = 0.2 \text{ revs per s}$$

$$12,000 \times 9.8 = 117600$$

$$P = 2\pi n T$$

$$F = F_r$$

$$= 12,000 \times 0.2$$

$$= 2400$$

$$P = 2\pi \times 320 \times 2400$$

$$T = F r$$

$$T = 117600 \times 0.2$$

$$T = 23520 \text{ Nm}$$

$$12 \div 60 = 0.2 \text{ revs per second}$$

$$T = F r$$

$$12,000 \times 9.8 = 117600 \text{ N}$$

$$r = 320 \div 2$$

$$r = 160$$

$$T = 117600 \times 160$$

$$T = 18816000 \text{ Nm}$$

$$P = 2\pi n T$$

$$P = 2\pi \times 0.2 \times 18,816,000$$

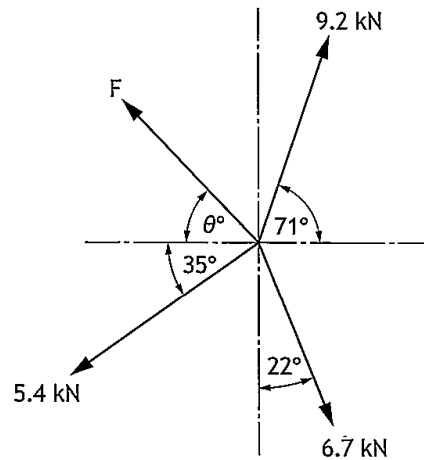
$$P = 23,644,882 \text{ W}$$

MARKS

## 11. (continued)

Later in the construction project, the lifting platform supports cables used to suspend a concrete beam above the site until it is ready for positioning.

The diagram below represents the concurrent force system while the beam is in suspension.



- (c) Calculate the magnitude and angle of the force  $F$ , required to maintain equilibrium.

6

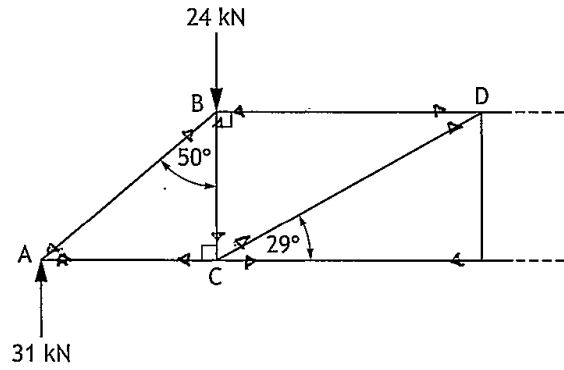
$$\begin{aligned} \sum F_V &= 0 \\ F \uparrow &= F \downarrow \\ 9.2 \sin 71^\circ + F &= 6.7 \sin 22^\circ + 5.4 \sin 35^\circ \\ 8.70 F &= 2.51 + 3.10 \\ F &= \frac{2.51 + 3.10}{8.70} \\ F &= 0.64 \text{ N} \end{aligned}$$

$$\begin{aligned} \sum F_H &= 0 \\ F \leftarrow &= F \rightarrow \\ 9.2 \cos 71^\circ + 6.7 \cos 22^\circ &= F \\ 2.99 + 6.21 &= 4.4 F \\ F &= \frac{2.99 + 6.21}{4.4} \\ F &= 2 \text{ N} \end{aligned}$$

$$\begin{aligned} R &= \sqrt{0.64^2 + 2^2} \\ R &= 2 \text{ N} \\ \theta &= \tan^{-1} \left( \frac{0.64}{2} \right) \\ \theta &= 17.74^\circ \\ \theta &= 18^\circ \end{aligned}$$

MARKS

12. The free-body diagram for part of a structure and its loading is shown below.



Calculate, using nodal analysis, the magnitude and nature of forces in members AB, AC, BC, BD and CD.

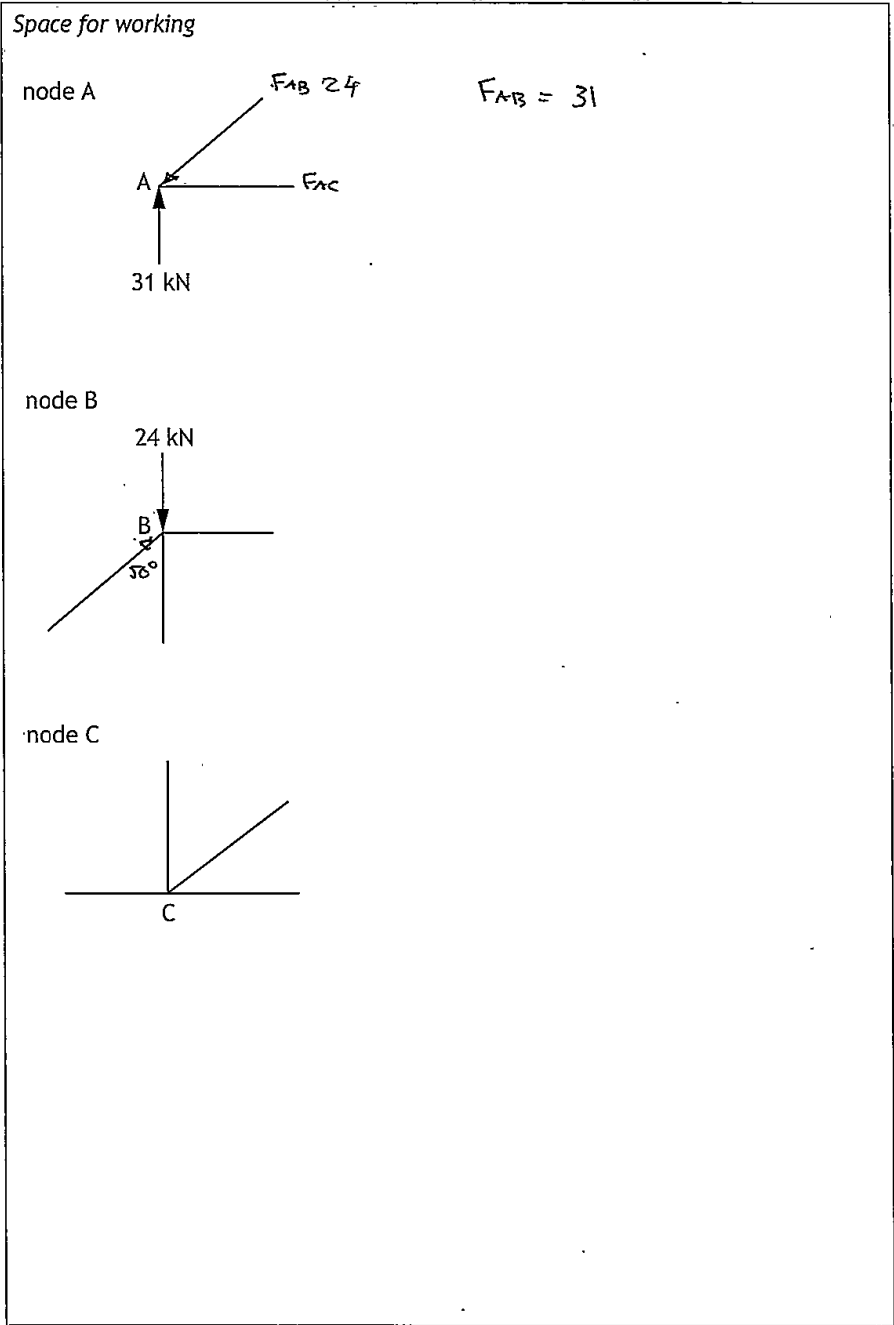
Show all working and final units on the page opposite.

Complete the table below.

8

Member	Magnitude	Nature
AB	7 kN	strut
AC	4.5 kN	tie
BC	6 kN	Strut
BD	8 kN	Strut
CD	3.2 kN	Tie

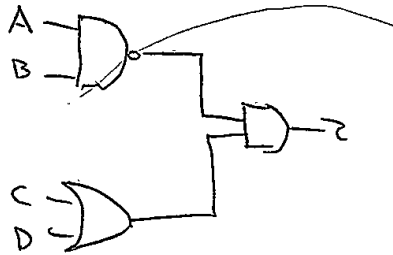
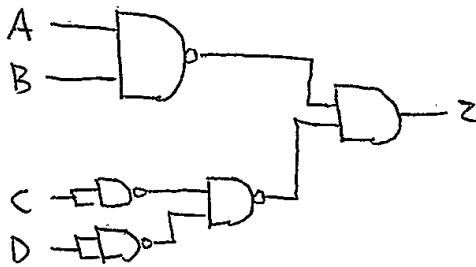
12. (continued)



[END OF QUESTION PAPER]

MARKS

Q6 
$$Z = (\overline{A \cdot B}) \cdot (C + D)$$

WorkingFinal answer

Q7

$$P = \frac{E}{t}$$

$$P = \frac{2885120}{11}$$

$$P = 262283 \text{ W}$$

Q8

$$E_p = mgh$$

$$E_p = 8163.27 \times 9.8 \times 15$$

$$E_p = 1,200,000 \text{ J}$$

$$0.87 \times 1,200,000$$

$$P_{\text{out}} = \underline{\underline{1,044,000 \text{ J}}}$$

$$80,000 \div 9.8$$

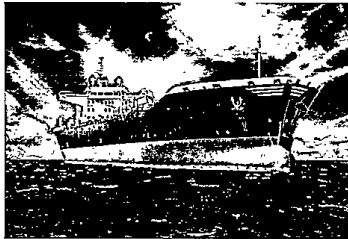
$$= 8163.27 \text{ kg}$$

# Candidate 3 evidence

**SECTION 1 — 20 marks**

Attempt ALL questions

1. A new material is being tested for use in the manufacture of ships.



The results of a tensile test on the material are shown in Figure 1.

The range of 0 to A is shown magnified in Figure 2.

Figure 1

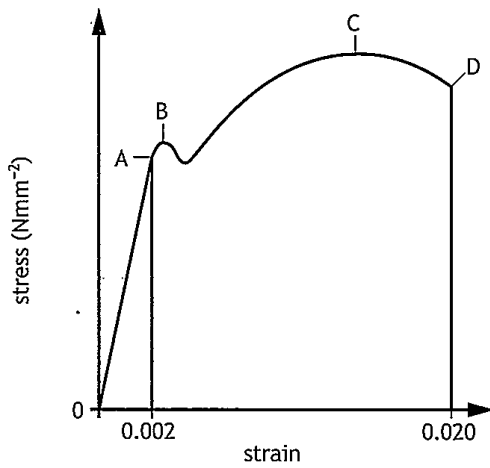
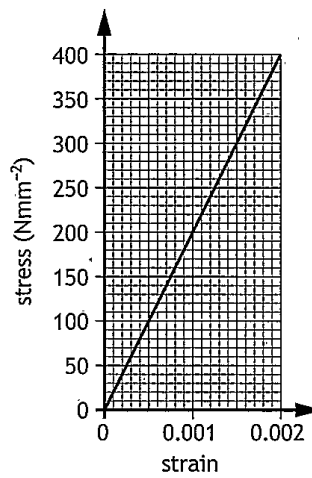


Figure 2



MARKS

## 1. (continued)

- (a) (i) State the name of the range 0 to A. 1  
elastic range
- (ii) State the name of the range A to D. 1  
plastic range
- (b) (i) Calculate, using the information from Figure 2, Young's Modulus for this material. 1

$$E = \frac{\sigma}{\epsilon} = \frac{400}{0.02}$$
$$E = 20,000 \text{ Nmm}^{-2}$$
$$E = \underline{20 \text{ kNmm}^{-2}}$$

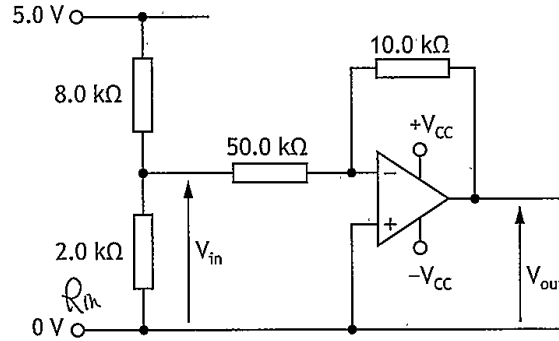
- (ii) State the property identified by point C on Figure 1. 1

ultimate tensile stress

[Turn over

MARKS

2. Part of an electronic circuit is shown.



(a) Calculate  $V_{out}$ .

1 - 2

2

0.5m4

$$V_{in} = \frac{2000}{10000} \times 5 = 1V$$

$$V_o = -\frac{R_f}{R_i} \times V_i$$

$$= -\frac{10,000}{20,000} \times 1$$

$$= -0.5 \times 1 = -0.5V$$

∴  $V_o = -0.5V$

0'

(b) Describe how the gain of this op-amp circuit could be decreased.

1

by decreasing the resistance of the reference resistor, by decreasing resistance of Rin resistor

After testing, it was decided to add an additional op-amp configuration to change the polarity of  $V_{out}$ .

(c) State the name of the op-amp configuration required to perform this task.

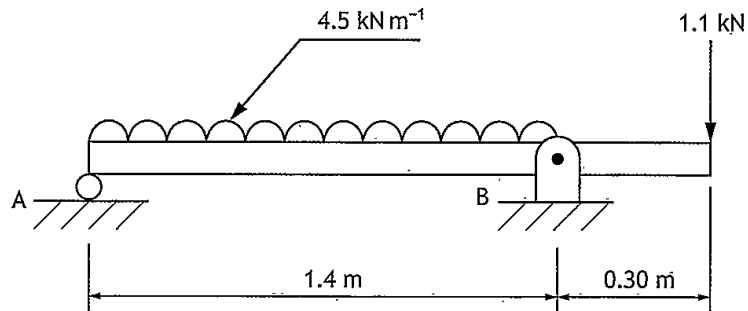
1

inverting amplifier



MARKS

3. A beam used in the construction of a covered walkway is shown.



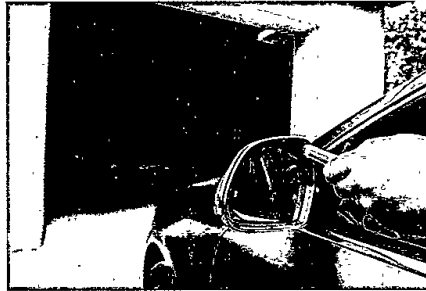
Calculate by taking moments about B, the vertical reaction at A.

3

$$\begin{aligned} \sum M_B &= 0 & \text{UDL} &= 4.5 \times 1.4 \\ & & &= 6.3 \text{ kN} @ 0.7 \text{ m} \\ R_A \times 1.7 &= (6.3 \times 0.7) + (1.1 \times 0.3) & & 4.74 \\ R_A \times 1.7 &= 4.41 + 0.33 \\ R_A &= 3.3857 \dots \text{ kN} \\ \underline{R_A} &= \underline{3.4 \text{ kN}} \end{aligned}$$

MARKS

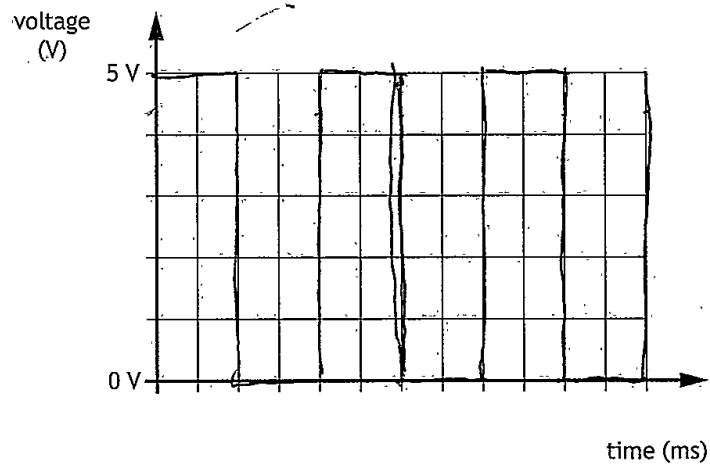
4. The speed at which an automatic garage door opens is controlled by a motor using pulse-width modulation (PWM).



- (a) Complete the graph below to show how PWM could be used to make the motor rotate at half speed.

You should include at least three pulses.

2



- (b) Describe how the speed of this motor could be decreased using PWM.

1

*by decreasing length of pulses (length of time of pulses)*

MARKS

## 4. (continued)

An alternative method of speed control involves varying the size of the DC voltage supplied to the motor.

- (c) Describe one advantage of using PWM in comparison to varying the size of the voltage supply.

1

more accurate and less wasted energy

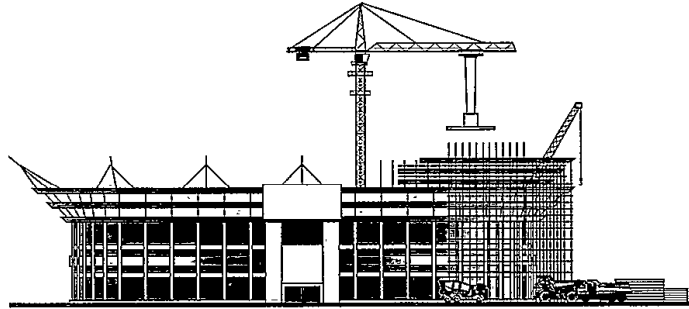
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---

[Turn over

MARKS

5. The capacity of a sports stadium is being increased. This needs an additional stand to be built on top of the existing structure.



A structural engineer is involved in the design of this new structure.

Describe two examples of how the structural engineer will use their knowledge of materials in the design of the new structure.

2

Example 1 Stresses and strains of preexisting materials to ensure that the stadium is not damaged or destroyed.

\_\_\_\_\_

\_\_\_\_\_

Example 2 Factor of safety is high enough to account for, poor workmanship, material anomalies and w, weather etc

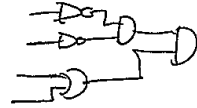
\_\_\_\_\_

\_\_\_\_\_

MARKS

6. An electronic engineer has designed a combinational logic circuit according to the Boolean equation, shown below.

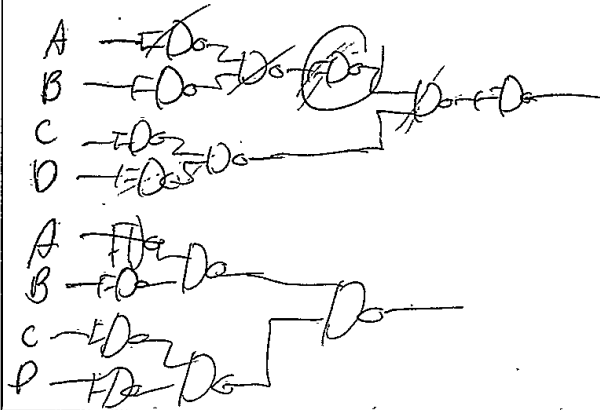
$$Z = (\overline{A \cdot B}) \cdot (C + D)$$



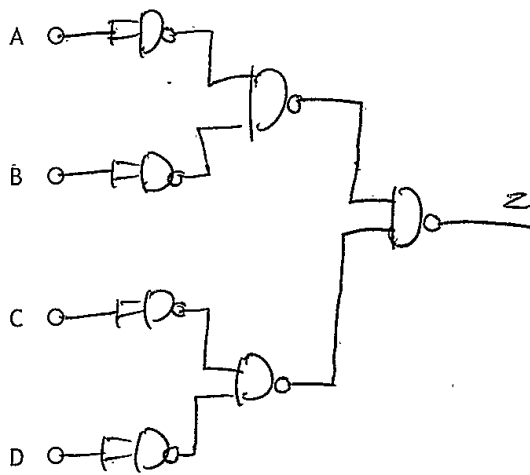
Draw a NAND equivalent circuit for this Boolean equation.

3

Space for working



Final answer

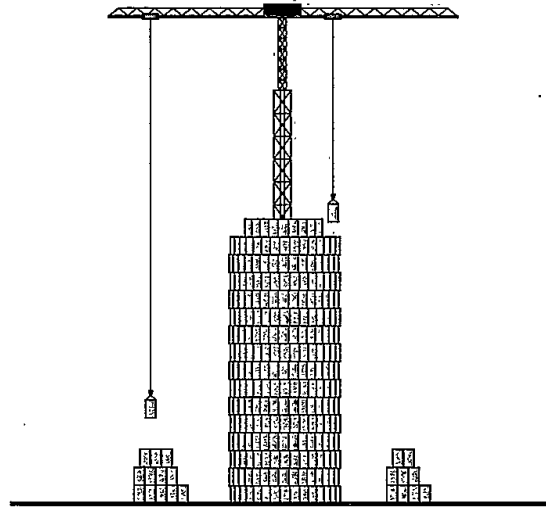


MARKS

## SECTION 2 — 90 marks

Attempt ALL questions

7. An engineering team has produced a prototype system to store excess energy from power plants.



When electricity production exceeds demand, electric motors are used to lift concrete blocks and place them in 'towers'. When the blocks are returned to ground level electricity is reclaimed by generators.

The first block has a mass of 10,000.0 kg. The system that raises this block is 92% efficient.

- (a) Calculate the energy required to raise this block 32 m.

0.08

2

$$\begin{aligned}
 E_p &= mgh && 250880 \\
 &= (10,000) \times (9.8) \times 32 \\
 &= 3136000 \\
 &&& 2885120 \\
 &&& \cancel{3136000} \\
 &&& 0.08 \times 3136000 \\
 &&& = 250880 \\
 3136000 - 250880 & \\
 &= 2885120 \\
 E &= 2.885 \text{ MJ} \\
 \underline{E} &= \underline{3136000}
 \end{aligned}$$

MARKS

## 7. (continued)

A second block applies a force of 80.0 kN to the supporting wire rope.

As this block is returned to ground level (at constant speed) its supporting wire rope turns a generator and electricity is reclaimed. This part of the system is 87% efficient.

- (b) Calculate the power output from the generator if this block descends 15 m in 11 seconds.

3

$$\begin{aligned}
 E &= Fd \\
 &= 80000 \times 15 \\
 &= 1.2 \text{ MJ} \\
 P &= \frac{E}{t} \\
 E &= Fd \\
 P &= \frac{E}{t} \\
 &= \frac{1200000}{11} \\
 &= 109090 \\
 P &= 109.09 \text{ kW} \\
 P &= 110 \text{ kW}
 \end{aligned}$$

The wire rope holding the 80.0 kN block as it is lifted is made from mild steel and has a diameter of 48 mm.

- (c) Calculate the factor of safety in the wire rope when it raises this block at a steady speed.

4

$$\begin{aligned}
 FOS &= \frac{UTS}{\sigma} \\
 FOS &= \frac{430}{\sigma} \\
 FOS &= 9.7263 \\
 FOS &= 9.7 \\
 &= 10 \\
 E &= \frac{\sigma}{\epsilon} \\
 E &= 196 \text{ kN/mm}^2 \\
 UTS &= 430 \\
 \sigma &= \frac{F}{a} = \frac{80000}{1809557} \\
 \sigma &= 44.20970643 \\
 \sigma &= 44.2 \text{ N/mm}^2
 \end{aligned}$$

## 7. (continued)

MARKS

- (d) Describe two economic and two environmental impacts that this system would have.

4

Economic impact 1 ~~if more~~ excess energy is storable then less money will be wasted producing ~~the~~ energy that will not be used.

Economic impact 2 lower prices of energy if storage is more efficient

Environmental impact 1 ~~if there is~~ less waste energy produced then less harm done to the environment when disposed of.

Environmental impact 2 \_\_\_\_\_

- (e) Describe two advantages that this system has over a chemical battery storage system for excess electrical energy.

2

Advantage 1 ~~to~~ accidents and chemicals ~~could be~~ chemical batteries are easily damaged

Advantage 2 \_\_\_\_\_



8. An anti-lock braking system is used to control the speed of an elevator as it descends. This uses a form of pulse-width modulation operated by a microcontroller.

If the speed of the elevator is too fast, the brakes will increase the proportion of operating time.

The table below identifies the connections to the microcontroller.

Input	Pin	Output
	7	brake
ground level sensor	1	
speed sensor (analogue)	0	

The system must perform the following steps.

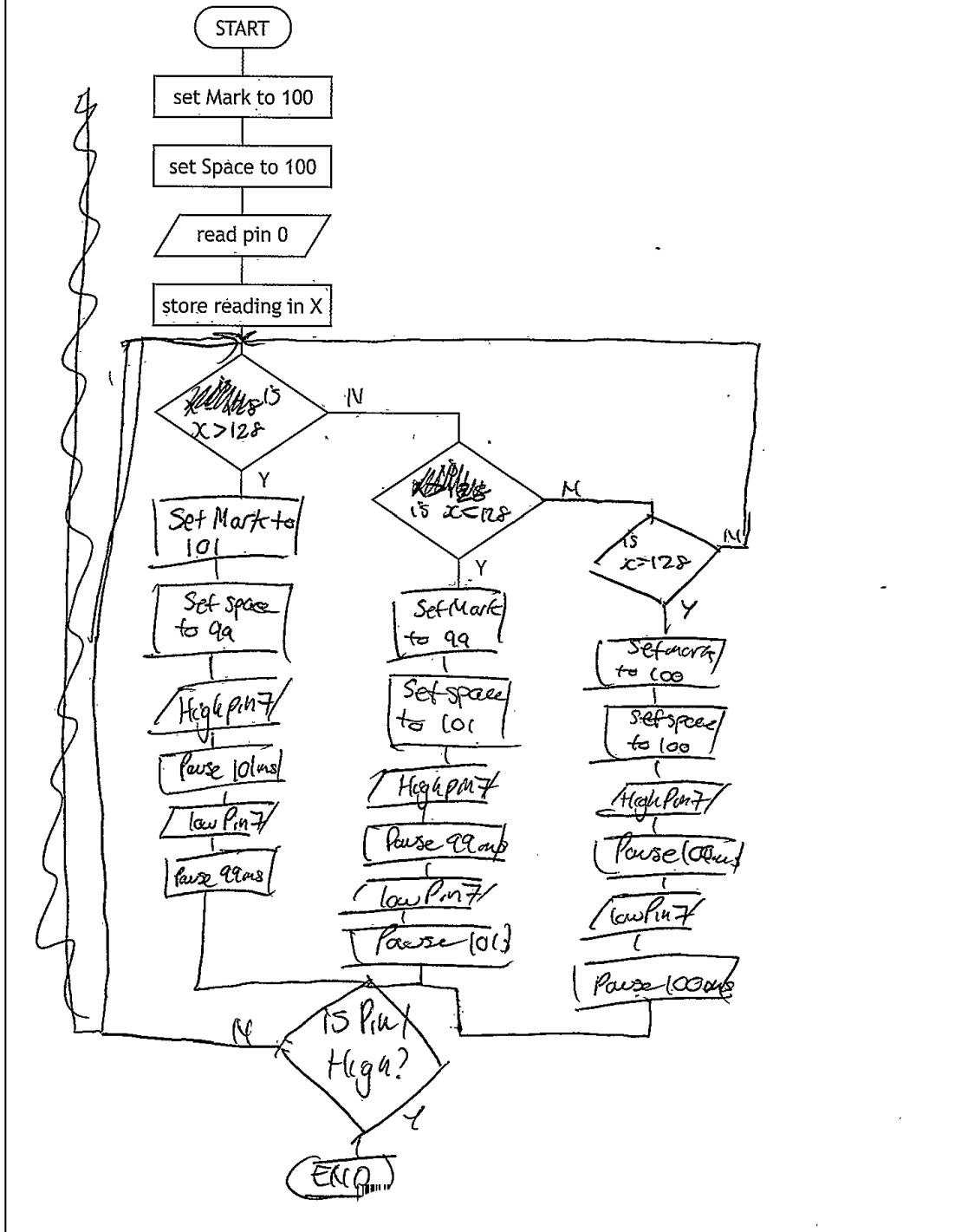
- Values for **mark** and **space** both need to be initially set to a value of 100
- A reading must be taken from a speed sensor and its value stored in variable X
- If the value of X is greater than 128 then **mark** increases by 1 and **space** decreases by 1
- If the value of X is smaller than 128 then **mark** decreases by 1 and **space** increases by 1
- If the value of X is 128 then **mark** and **space** do not change
- The brake must be switched on and off for the times specified **mark** and **space** (this will be in milliseconds)
- The process must continue until the ground level sensor is activated

MARKS

8. (continued)

(a) Complete, with reference to the specification and the input/output table, this flow chart for the control of the system.

8



MARKS

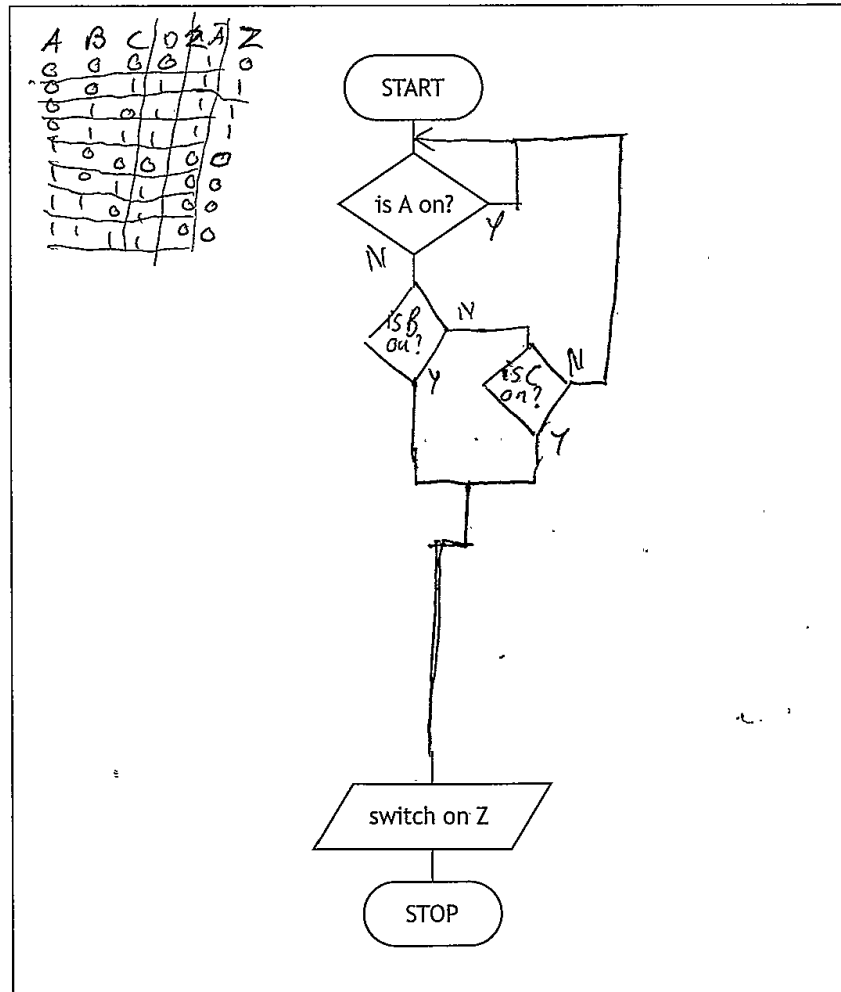
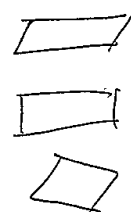
8. (continued)

An alarm (Z) is part of the elevator's operating system and needs to be activated under the conditions given by the following Boolean equation.

$$Z = \bar{A} \cdot (B + C)$$

(b) Complete the following flowchart to perform the function described above. 3

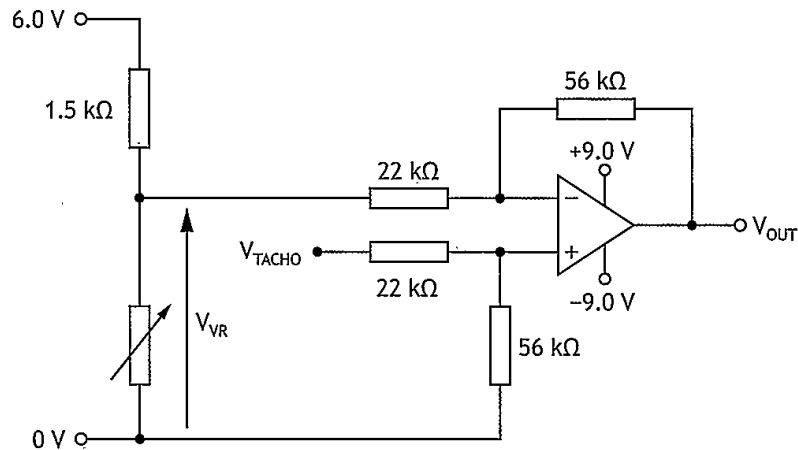
A needs to be 0 for Z to be 1



MARKS

8. (continued)

An alternative system to control the force applied by the brake is also tested. As the speed of the elevator varies from a reference value the output of the circuit changes proportionately. The speed of the elevator is monitored by a tachogenerator.



When testing the circuit, the voltage from the tachogenerator ( $V_{TACHO}$ ) was found to be 2.3 V.

- (c) (i) Calculate the resistance of the variable resistor in the circuit shown above when the output voltage of the op-amp is +4.5 V.

4

99000

1.7

1.77

795

5.47

1.47

$$V_o = \frac{R_f}{R_i} (V_2 - V_1)$$

$$4.5 = \frac{56k}{22k} (2.3 - V_{VR})$$

$$2.3 - V_{VR} = \frac{4.5 \times 22k}{56k}$$

$$V_{VR} = 2.3 - 1.76785$$

$$= 0.53V$$

$$R_{VR} = 145.2 \Omega$$

$V_2 = 2.3V$

$V_1 = V_{VR}$

$R_f = 56k \Omega$

$R_i = 22k \Omega$

$V_o = 4.5V$

$R_1 V_2 = V_1 R_2$

$R_2 = \frac{R_1 V_2}{V_1}$

$R_2 = \frac{22k \times 2.3}{0.53}$

$R_2 = 96.2283 \Omega$

$V = IR$      $3.65 \mu A$

$I = \frac{V}{R} = \frac{5.47}{1500}$

$V = IR$      $V = 0.53$

$R = \frac{V}{I} = \frac{0.53}{3.65 \times 10^{-6}}$

$R = 145.2 \Omega$      $2.3 - 0.51$

MARKS

8. (c) (continued)

- (ii) Describe, with reference to the circuit, how the reference speed of the elevator could be increased.

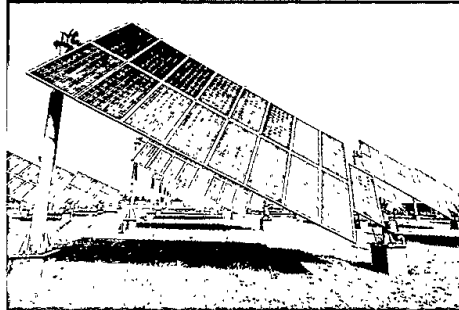
1

increasing the value of

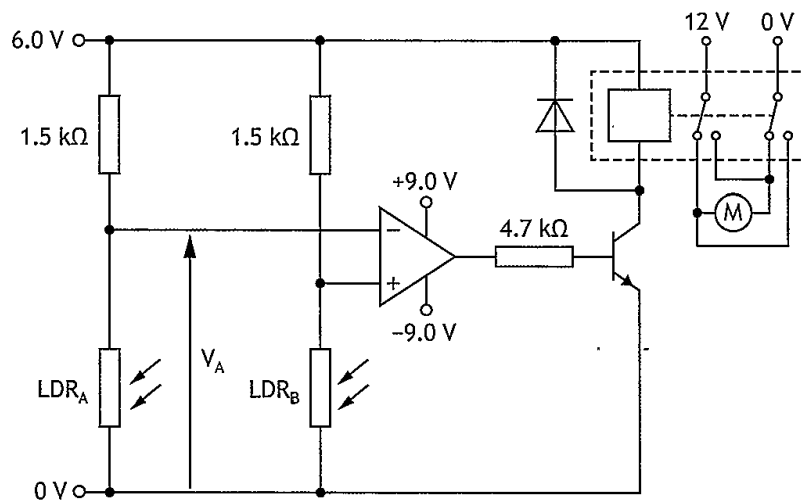
decreasing the value of the variable resistor  
decreases  $V_R$  which increases the difference  
between  $V_{ACRO}$  and  $V_{VE}$ , increasing  
 $V_{out}$  and the speed of the elevator

[Turn over

9. A system is needed to alter the position of a solar panel so that it is constantly facing the sun during daylight hours. If one sensor gives a higher reading than the other, a motor will turn the panel in the brighter direction.



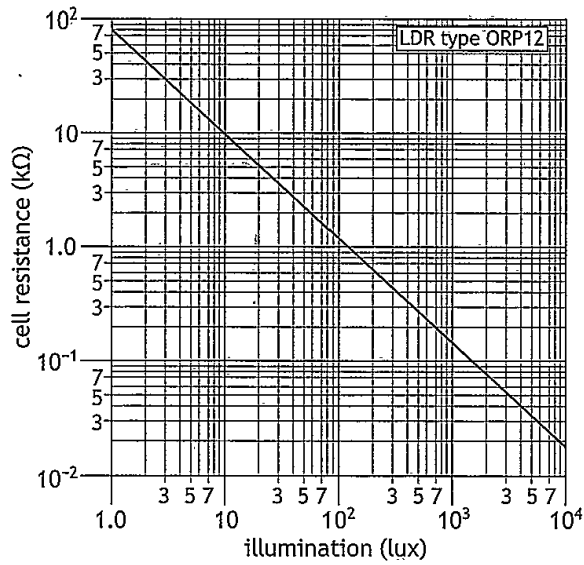
A preliminary design of the control circuit is shown below.



MARKS

9. (continued)

The characteristics of the LDRs are shown in the graph below.



(a) Calculate  $V_A$  if the light level on  $LDR_A$  is 20 lux.

0.0093

2

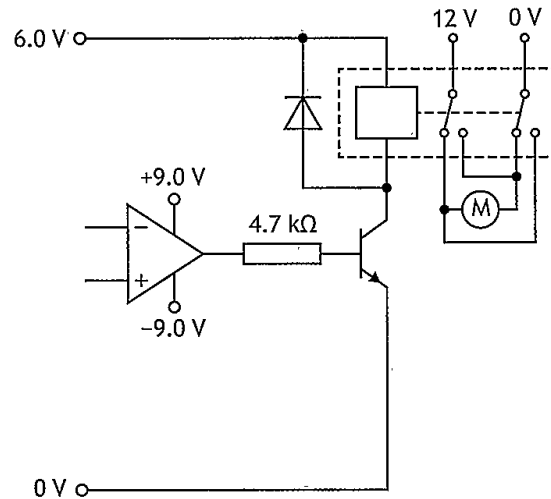
Handwritten student work for part (a):

$5k\Omega$   
 $\frac{R}{V_{0.0093}} = \frac{5000}{0.0093}$   
 $V_A = 4.62V$   
 $V_A = 4.6V$   
 $V_A = 4.6V$   
 $V_0 = \frac{5000}{0.0093} \times 6$   
 $V_A = 4.6V$   
 $I = \frac{V}{R}$   
 $I = \frac{4.6}{5000}$   
 $I = 0.92mA$

MARKS

9. (continued)

Part of the control circuit is shown below.



- (b) (i) Calculate the base current to the transistor when the op-amp saturates positively.  
 Assume  $V_{be}$  is 0.70 V. The op-amp output saturates at 75% of the supply voltage.

3

$$V = IR$$

$$I = \frac{V}{R} = \frac{(6.75 - 0.7)}{4700} = 0.75 \times 9 = 6.75V$$

$$I = 1.287 \times 10^{-3}$$

$$I_b = 1.3mA$$

$0.75 \times 9 = 6.75V$   
 $0.13 \times 10^{-2}$   
 $0.0013$   
 $0.0013A$



MARKS

## 9. (b) (continued)

The relay has a resistance of  $5.0 \Omega$ .

- (ii) Calculate the minimum current gain of the transistor to ensure it is fully saturated when the op-amp is saturated positively.

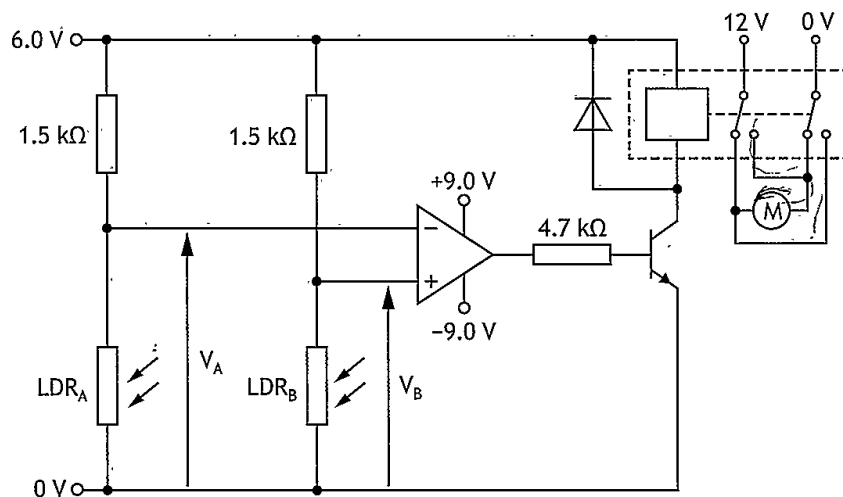
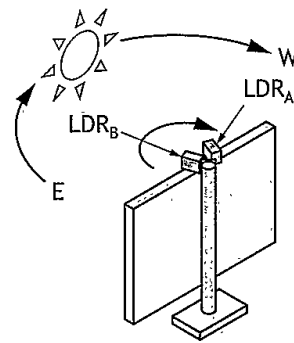
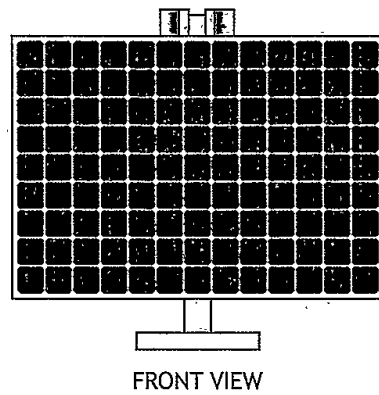
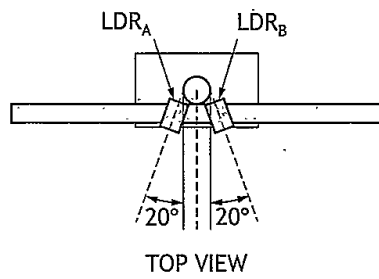
2

$$\begin{aligned} h_{fe} &= \frac{I_c}{I_b} \\ &= \frac{1.24}{0.00134} \\ &= 923.07 \\ \underline{h_{fe}} &= \underline{920} \end{aligned}$$
$$\begin{aligned} V &= IR \\ I &= \frac{V}{R} = \frac{6}{5} \\ I_c &= 1.24 \end{aligned}$$

[Turn over

9. (continued)

While testing the circuit,  $V_A$  was found to be less than  $V_B$  and the motor rotated, moving the solar panel towards the sun's position.



MARKS

## 9. (continued)

- (c) Describe, referring to the circuit on the opposite page, what will happen as the solar panel moves.

Your answer must refer to the input voltage dividers, the op-amp and transistor, and the relay and motor.

6

Input voltage dividers as light levels decrease, resistance of LDRs increases,  $V_A$  which increases voltage output. depending on which side is darker, the larger output is given and motor.  
if  $V_A < V_B$  then the op amp saturates positively and turns on if  $V_A > V_B$  then the op amp saturates negatively

Op-amp and transistor

if output voltages of  $V_A$  and  $V_B$  are equal or close enough that an output is put out that is less than 0.7V but larger than -0.7V then the motor will not turn

Relay and motor depending on ~~the~~ saturation state of the op amp ~~state~~ DPDT is switched depending on polarity of electromagnetic field produced by relay

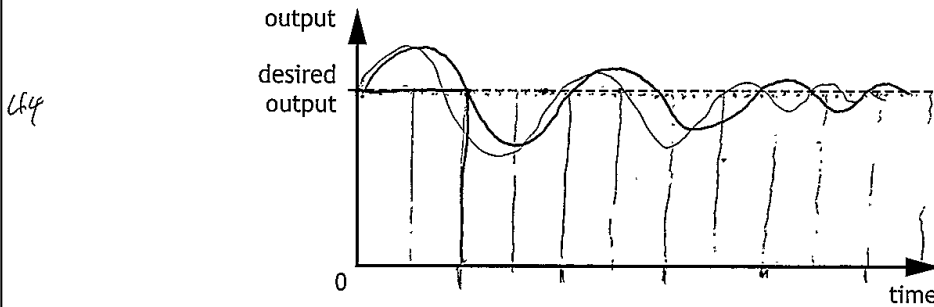
[Turn over

MARKS |

## 9. (continued)

The op-amp control circuit uses two-state control.

- (d) (i) Complete the graph below to show how the output of a two-state control system changes as it approaches the desired output. 2



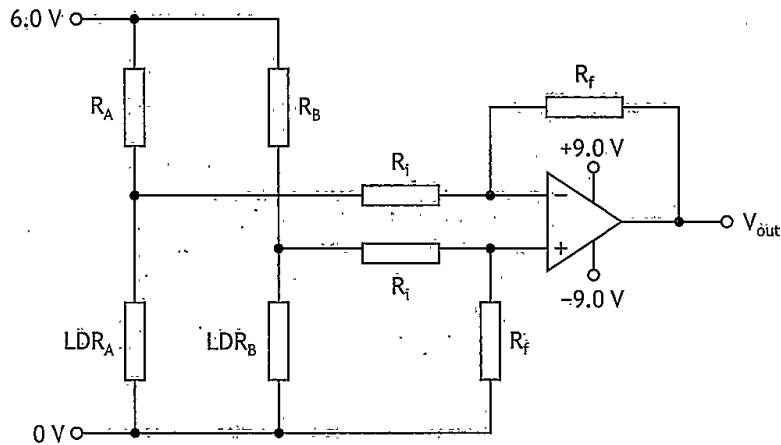
- (ii) Describe the impact that this type of control would have on the mechanical output of the system. 1

the change output would change less  
and less as it gets closer to  
desired output

MARKS

9. (continued)

An alternative control circuit is also tested.



- (e) (i) State the type of control produced by this type of circuit.

1

*closed loop feedback*

- (ii) Describe the difference between the control produced by this circuit and a two-state control system. You can use diagrams or graphs to illustrate your answer.

3

[Turn over]

MARKS

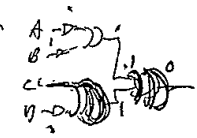
10. An engineering team is experimenting with different control systems to operate a number of pneumatic cylinders. The following truth table shows the conditions under which one of the cylinders must outstroke.

A	B	C	D	Z
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

D

→

Z = (when C=1)



- (a) Write a Boolean equation for the output Z.

2

Z = \_\_\_\_\_

\_\_\_\_\_

MARKS

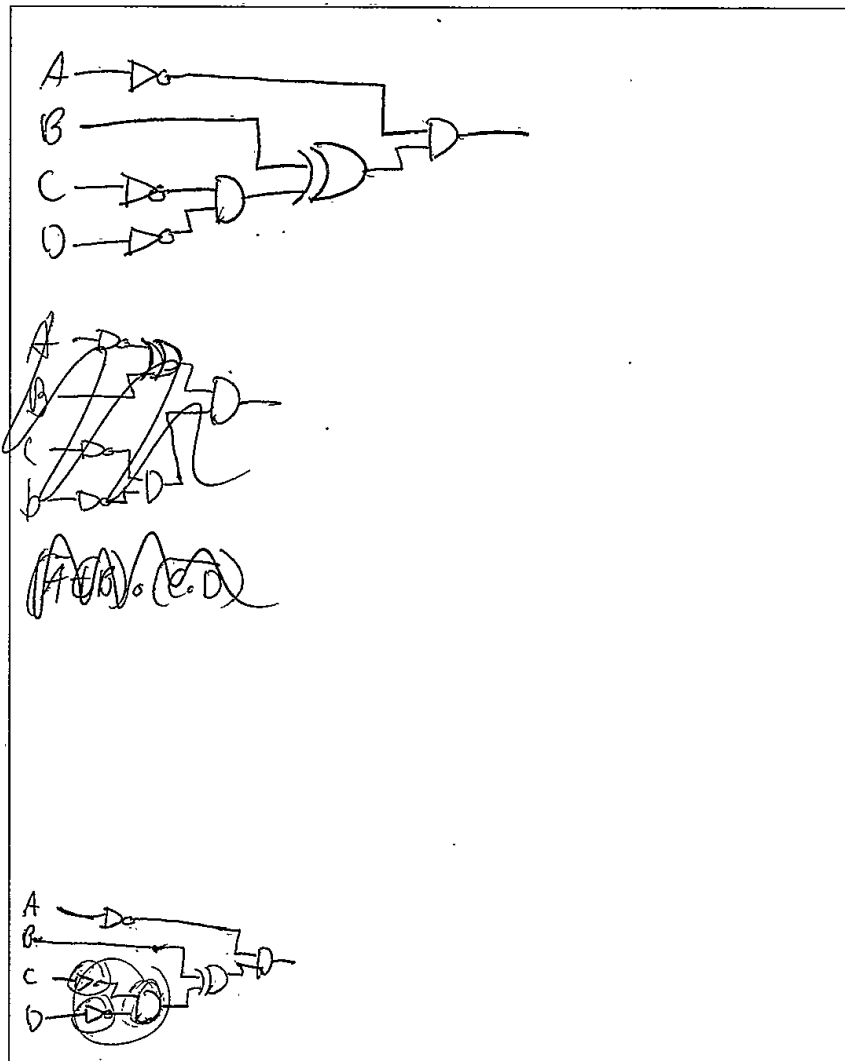
10. (continued)

A second cylinder operates under the following conditions.

$$X = \bar{A} \cdot B \oplus (\bar{C} \cdot D)$$

(b) Draw a logic diagram to perform this function.

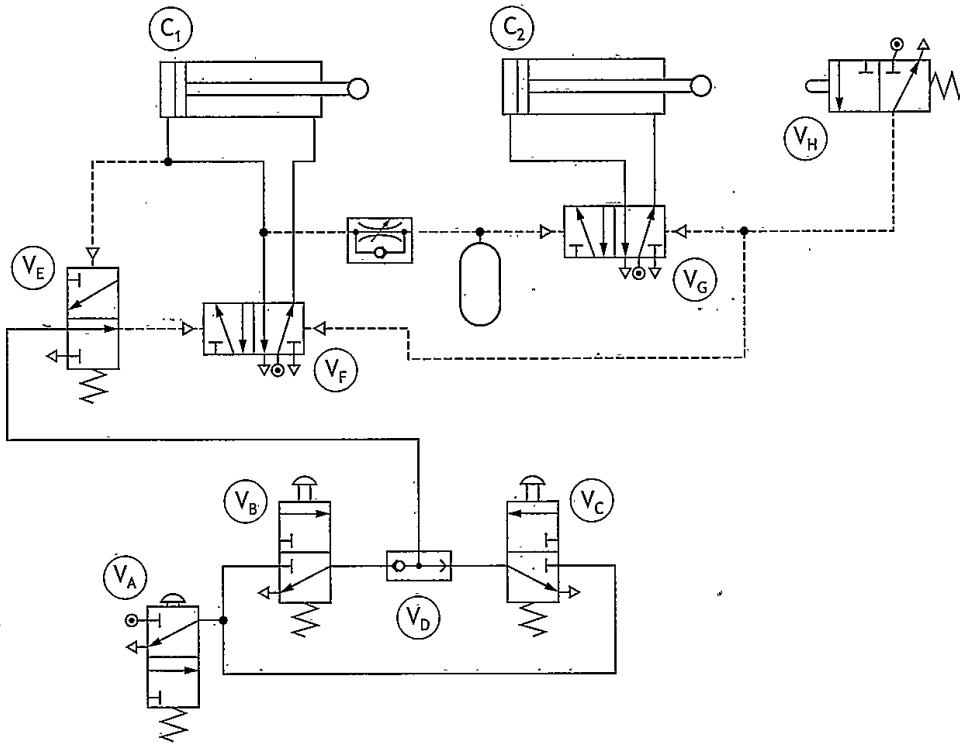
4



[Turn over

10. (continued)

Two further cylinders are to be controlled by the following circuit.





MARKS

## 10. (continued)

- (c) (i) Describe the operation of this circuit, highlighting the function of each component and the conditions that will cause the cylinders to instroke and outstroke.

6

When  $V_A$ ... is in its <sup>Top</sup> ~~bottom~~ state and  $V_B$  is in its bottom state then the  $V_D$  is pushed right. ~~When  $V_B$  is in its bottom state~~ flows through  $V_E$  putting  $V_F$  into its left hand state, causing  $C_1$  to outstroke. air flows through ~~the  $V_D$  and  $V_F$~~   $V_D$  and reservoir causing a time delay, then  $V_G$  is put into its left hand state, causing  $C_2$  to ~~retract~~ and outstroke and activate  $V_H$  which ~~then~~ puts  $V_G$  and  $V_F$  back into their right hand states. ~~the and  $V_B$ ,  $V_C$  and  $V_D$  act as an XOR gate, if one is activated then air flows in none or both are activated then air does not flow~~

The engineering team are considering changing the circuit shown opposite to one that is operated by a microcontroller.

- (ii) Describe two reasons why using a microcontroller-based system is preferred to a fully pneumatic system.

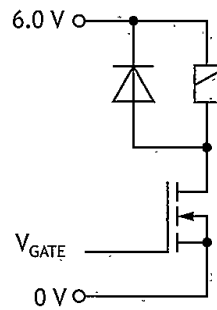
2

~~allows for more~~ ~~control~~ ~~of the~~ easier to control and make alterations

MARKS

10. (continued)

In order to use a microcontroller-based system, solenoid valves need to be used. The following circuit has been designed to actuate one of the solenoids.



The solenoid is rated 12 W at 6.0 V. The MOSFET has a resistance of 0.70 Ω when switched on.

- (d) (i) Calculate the resistance of the solenoid.

1

$$\begin{aligned}
 P &= IV \\
 P &= \frac{V^2}{R} \quad R = \frac{V^2}{P} = \frac{36}{12} = 3\Omega \\
 I &= \frac{P}{V} = \frac{12}{6} = 2A \\
 I &= \frac{V}{R} \quad R = \frac{V}{I} = \frac{6}{2} = 3\Omega
 \end{aligned}$$

*Handwritten notes:*  $P = I^2 R$ ,  $V = IR$ ,  $R = \frac{V}{I} = \frac{6}{2} = 3\Omega$ ,  $R = 3.7\Omega$ ,  $R = 3\Omega$

- (ii) Calculate the current through the MOSFET when it is fully switched on.

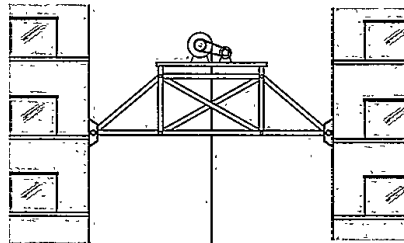
1

$$\begin{aligned}
 V &= IR \\
 V &= IR \\
 I &= \frac{V}{R} = \frac{6}{2.3} = 2.6A \\
 R_{\text{MOSFET}} &= 3 - 0.7 = 2.3
 \end{aligned}$$

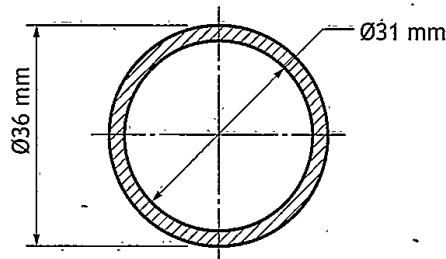
*Handwritten notes:*  $V = IR$ ,  $R_{\text{MOSFET}} = 3 - 0.7 = 2.3$ ,  $I = \frac{V}{R} = \frac{6}{2.3} = 2.6A$

MARKS

11. During a construction project in a city centre location, a lifting platform is installed between two high rise buildings.



One of the members in the structure has a cross-section as shown below, with an internal diameter of 31 mm, and an external diameter of 36 mm.



$E =$

This mild steel member has a strain of  $4.6 \times 10^{-5}$  when subjected to a load.

- (a) Calculate the load carried by this member.

1296  
754.767635

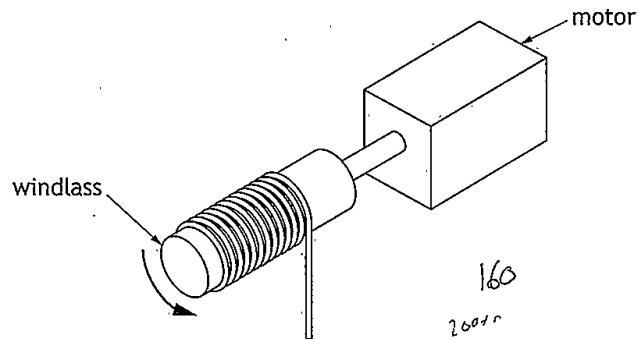
969 1017.87602 4

$E = \frac{\sigma}{\epsilon}$ $\sigma = E \times \epsilon$ $= 196000 \times 4.6 \times 10^{-5}$ $\sigma = 9.016$ $\sigma = \frac{F}{A} \quad F = \sigma \times A$ $F = 9.016 \times 2361$ $F = 21286.776$ $F = \underline{\underline{2.13 \text{ kN}}}$	$A = \frac{\pi d^2}{4} - \frac{\pi d^2}{4}$ $A = 1017.87602 - 754.767635$ $A = 263.108385$ $A = 236.1 \text{ mm}^2$ $E = 196 \text{ kN/mm}^2$
---	---

MARKS

## 11. (continued)

A motor-driven winch system is used for lifting construction materials with up to 12,000 kg of mass. The windlass, with 320 mm diameter, rotates at 12 revolutions per minute.



(b) Calculate the mechanical power required by this motor.

5

$$P = 2\pi nT$$

$$P = 2 \times \pi \times 0.2 \times T$$

$$P = 428261.9105$$

$$P = 428.26 \times 10^3$$

$$\underline{P = 430 \text{ kW}}$$

$$n = \frac{12}{60} = 0.2 \text{ revs/sec}$$

$$m = 12000 \text{ kg}$$

$$d = 320 \text{ mm}$$

$$T = F \times r$$

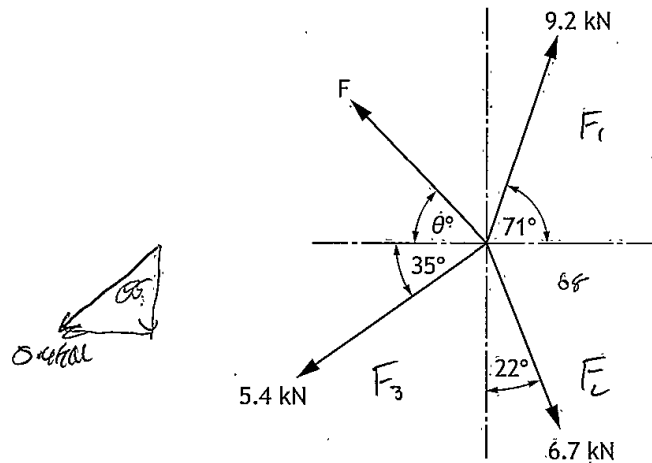
$$= 340800$$

MARKS

11. (continued)

Later in the construction project, the lifting platform supports cables used to suspend a concrete beam above the site until it is ready for positioning.

The diagram below represents the concurrent force system while the beam is in suspension.



- (c) Calculate the magnitude and angle of the force  $F$ , required to maintain equilibrium.

6

~~$\sum F = \sum F$~~

~~$F_1 + 9.2 \sin 71 = 5.4 \sin 35 + 6.7 \sin 22$~~   $5.16071$

~~$F_1 + 8.69877 = 3.0973 + 2.5098$~~

~~$F_1 = 9.3093 - 8.69877$~~

~~$F_1 = 0.61053$~~

~~$F_1 = 0.61 kN$~~

610

1082

1170724

372100

1542824

$\sum \rightarrow F = \sum \leftarrow F$

$F_1 + 5.4 \cos 35 = 6.7 \cos 68 + 9.2 \cos 71$

$F_1 + 4.423 = 2.50986 + 2.995$

$F_1 = 5.5065 - 4.423$

$F_1 = 1.082 kN$

$\tan \theta = \frac{v}{h}$

$\theta = 29.44^\circ$

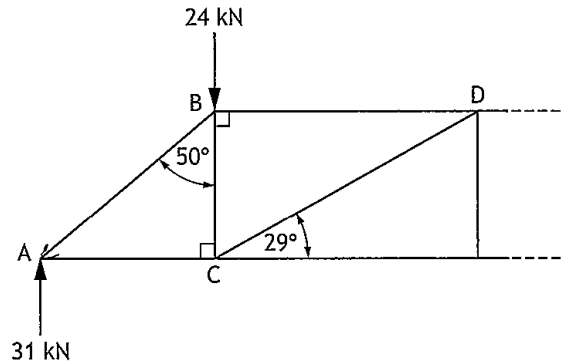
$|F| = \sqrt{F_1^2 + F_2^2}$

$F = 12.42$

$F = 12.26 kN$

MARKS

12. The free-body diagram for part of a structure and its loading is shown below.



Calculate, using nodal analysis, the magnitude and nature of forces in members AB, AC, BC, BD and CD.

Show all working and final units on the page opposite.

Complete the table below.

8

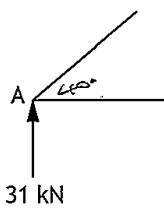
Member	Magnitude	Nature
AB	68.2 kN	strut
AC	36.9 kN	tie
BC	24 kN	strut
BD	36.9 kN / 31 kN	
CD	27.6 kN	TIE

~~68.2 kN~~

12. (continued)

Space for working

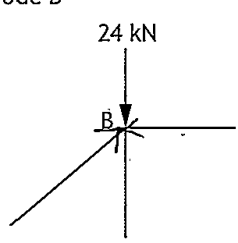
node A



$\sum \uparrow F = \sum \downarrow F$   
 $31 \text{ kN} = F_{ABV}$   
 $F_{AB} \sin 40 = 31$   
 $F_{AB} = 48.227$   
 $F_{AB} = 48.2 \text{ kN}$   
 (STRUT)

$\sum \rightarrow F = \sum \leftarrow F$   
 $F_{ABH} = F_{AC}$   
 $F_{AC} = 48.2 \cos 40$   
 $F_{AC} = 36.923$   
 $F_{AC} = 36.9 \text{ kN}$   
 (TIE)

node B

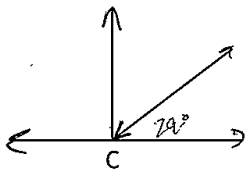


$\sum \uparrow F = \sum \downarrow F$   
 $F_{BC} = 24 \text{ kN}$   
 (STRUT)

$\sum \rightarrow F = \sum \leftarrow F$   
 $F_{BDH} = F_{BD}$   
 $F_{BD} = 48.2 \cos 40$   
 $F_{BD} = 36.9 \text{ kN}$

$F_{BD} = 48.2 \cos 50$   
 $F_{BD} = 30.98$   
 $F_{BD} = 31 \text{ kN}$

node C



$\sum \uparrow F = \sum \downarrow F$   
 $F_{BC} = F_{CDV}$   
 $F_{CD} \sin 29 = 24$   
 $F_{CD} = 49.57 \text{ kN}$

$\sum \rightarrow F = \sum \leftarrow F$   
 $F_{BC} = F_{CDH}$   
 $F_{CD} \cos 29 = 24$   
 $F_{CD} = 27.04 \text{ kN}$

[END OF QUESTION PAPER]

ENTER  
NUMBER  
OF  
QUESTION

and the use of PPM Counter  
would need to be adapted  
as ~~this is only good~~ to currents  
only works for integers,  
perhaps if the program was  
upscaled so it checked over  
more than 35, then an  
accurate reading could then  
be made by incrementing  
with smaller decimal  
values.